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# **Innovation & Trends In Missing Data Sensitivity Analyses**

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# Outline

- **Background**
- **New approaches**
- **Example**

# Current State

- **NRC panel convened at request of FDA. Strong agreement among stake holders**
- **Recommendations include**
  - **Clear objectives**
  - **Maximize retention**
  - **Sensible primary analysis supported by sensitivity analyses**
  - **Need for further research on sensitivity analyses and how to use them to draw inference**
    - **DIASWG**



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## DIA working group

The following pages contain materials available from the Drug Information Association (DIA) working group.

Please note that these pages are still under construction.

- **Descriptive Summaries** ( 1 Article )
- **Inclusive Modeling Approaches** ( 4 Articles )
- **Missing Not at Random (MNAR) Methods** ( 4 Articles )
- **Control-Based Multiple Imputation** ( 3 Articles )
- **Presentations, Manuscripts and Training Materials** ( 2 Articles )
- **Example Datasets** ( 1 Article )

# Missing Data Mechanisms

- **MCAR**: Conditional on the independent variables in the model, neither observed or unobserved outcomes of the dependent variable explain dropout
- **MAR**: Conditional on the independent variables in the model, observed outcomes of the dependent variable explain dropout, but unobserved outcomes do not

# Missing Data Mechanisms

- **MNAR**: Conditional on the independent variables in the model and the observed outcomes of the dependent variable, the unobserved outcomes of the dependent variable explain dropout
- Alternatively, in **MNAR**, conditional on the covariates and observed outcomes, the **statistical behavior** of the **unobserved data** is **not equal** to that if it had been observed
  - In MAR it is equal

# Missing Data in Clinical Trials

- Efficacy outcomes are seldom MCAR because the observed outcomes typically influence dropout (discontinue for lack of efficacy)
- Trials are designed to observe all the relevant information, which minimizes MNAR data
- Hence in the highly controlled scenario of longitudinal confirmatory trials, missing data may be mostly MAR – or at least MAR provides a good starting point
- **MAR often plausible, but never provable.** Particular MNAR model never provable either

# General Guidance

- **Strive for validity of MAR**
  - **Maximize retention**
  - **Capture data predictive of drop out**
  - **MAR primary analysis options include**  
**MI, likelihood-based, wGEE**
- **Assessing consequences of departures from MAR is the cornerstone of sensitivity analyses**



# Established MNAR Methods

- **General classes of MNAR methods based on factorizations of the likelihood functions for the joint distribution of the outcome variable and the indicator variable for whether or not a data point is observed**
- **Factorization in this context means that the hypothetical “full” data are split into two parts: the actually observed and the missing**
  - *Shared parameter model*
  - *Selection models*
  - *Pattern mixture models*

# Selection Model

- $f(Y_i, R_i | \theta, \Psi) = f(Y_i | \theta) f(R_i | Y_{o_i}, Y_{m_i}, \Psi)$
- The joint distribution of the  $i$ th patient's outcomes ( $Y_i$ ) and the missingness indicators ( $R_i$ ) is factored as the marginal distribution of  $Y_i$  and the conditional distribution of  $R_i$  given  $Y_i$
- Assume:
  - Full-response data comprise  $(Y_1, Y_2)$
  - Objective is to compare  $Y_2$  means
  - $Y_2$  is missing on some individuals

# Notation

Subject  $i$  is to be measured at times  $j = 1, \dots, n$

$Y_{ij}$  = measurement on subject  $i$  at time  $j$ ,  $j = 1 - n$

$R_{ij}$  = indicator variable = 1 if  $Y_{ij}$  observed, 0 otherwise.

Group  $Y_{ij}$  into a vector  $Y_i = (Y_{o_i}, Y_{m_i})$

$Y_{o_i}$  contains  $Y_{ij}$  for which  $R_{ij} = 1$ ,

$Y_{m_i}$  contains  $Y_{ij}$  for which  $R_{ij} = 0$ .

Group  $R_{ij}$  into a vector  $R_i$  commensurate with  $Y_{ij}$  such that all 1s are paired with the  $Y_{o_i}$  and the 0s are paired with the  $Y_{m_i}$

$\Psi$  = Parameters describing missingness process

$\theta$  = Parameters describing measurement process

# Selection Model

- **No info on association b/t R and  $Y_2$  because  $Y_2$  is always missing when  $R = 0$**
- **Can fit model even though no empirical information on some parameters b/c of the parametric and structural assumptions imposed**
- **Standard recommendations are to input values of this parameter(s) across a plausible range and assess consistency of the difference between group means for  $Y_2$**

# Caveats

- How do we determine plausible range?
- How do we determine dropout model?
  - Same or different for each treatment?
  - Same or different for each time point
  - **MNAR methods are sensitive to model misspecification**
- **Never have data to inform these choices**

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# Modeling Alternative: Doubly Robust Methods

- **Protects against mis-specified dropout model**
  - **3 Parts: 1) analysis model, 2) dropout model, 3) model for the joint distribution of the partially and fully observed data (compatible with 1)**
  - **If either model 2 or 3 is wrong, but not both, the estimators in 1 are still consistent**
  - **If model 1 is wrong, e.g., because a key confounder is omitted, then estimates of all parameters will typically be inconsistent**
- **Some implementations are complex**
- **Need more experience**
- **Macro available at [missingdata.org.uk](http://missingdata.org.uk)**

# Another Alternative: Controlled Imputations

- Assumptions can be transparent, debated, **and evaluated**
- Tweak on standard MI, implement w standard software
- General idea is to create specific and relevant departures from MAR
  - Reference-based: Plausible worst case
  - Delta-adjustment: Progressive stress test
  - Several implementations of each allows fit for purpose

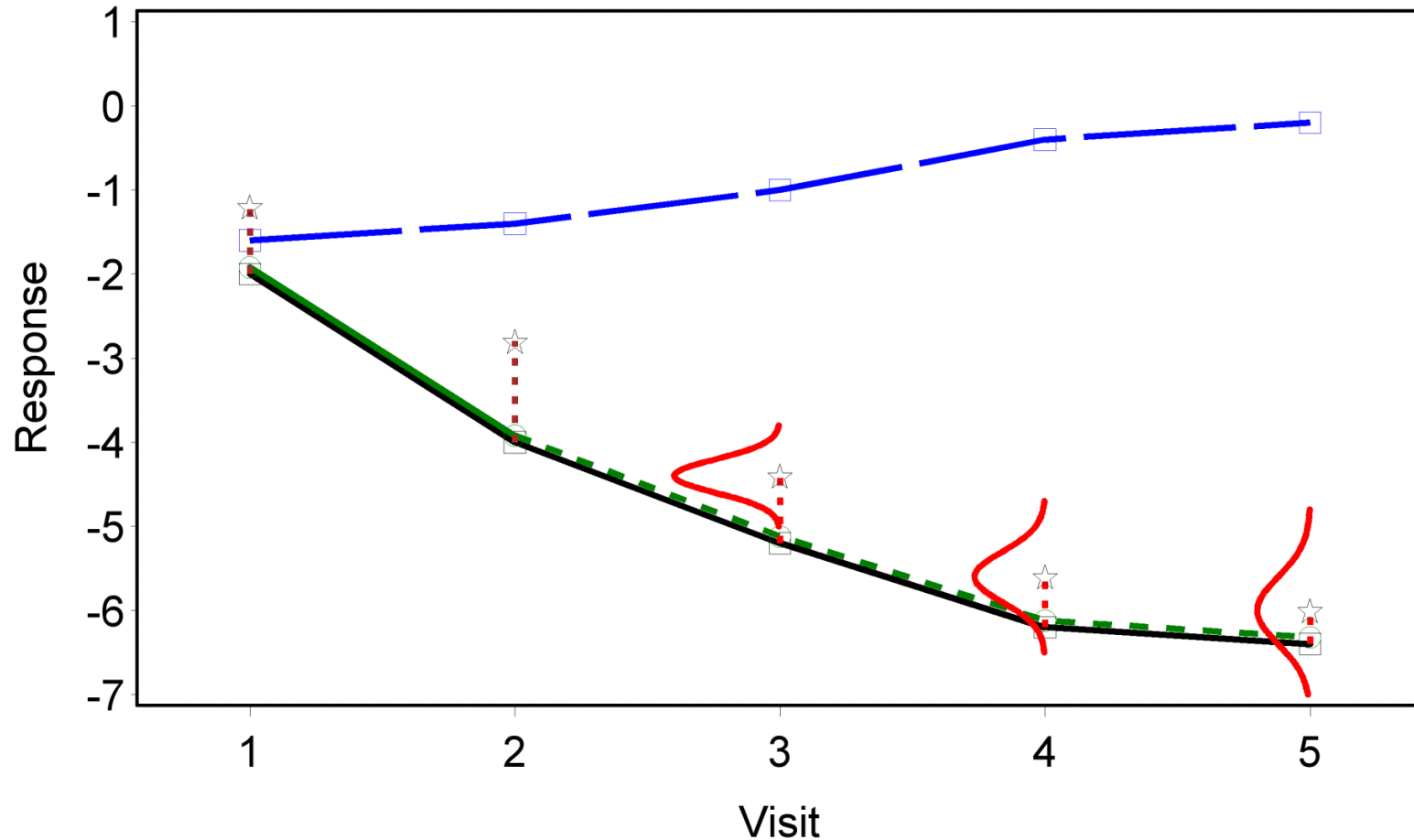


# Controlled Imputations: Reference Based

- **Copy increment from reference (CIR)**
  - After dropout, change for drug = change for placebo
    - Use for disease modifying drugs
- **Copy reference (CR)**
  - The statistical behavior of drug treated patients after dropout **gradually transitions** to reference arm
    - Use for drugs with long on target half life
- **Jump to reference (J2R)**
  - **...immediately becomes** that of reference patients
    - Use for drugs with short on target half-life

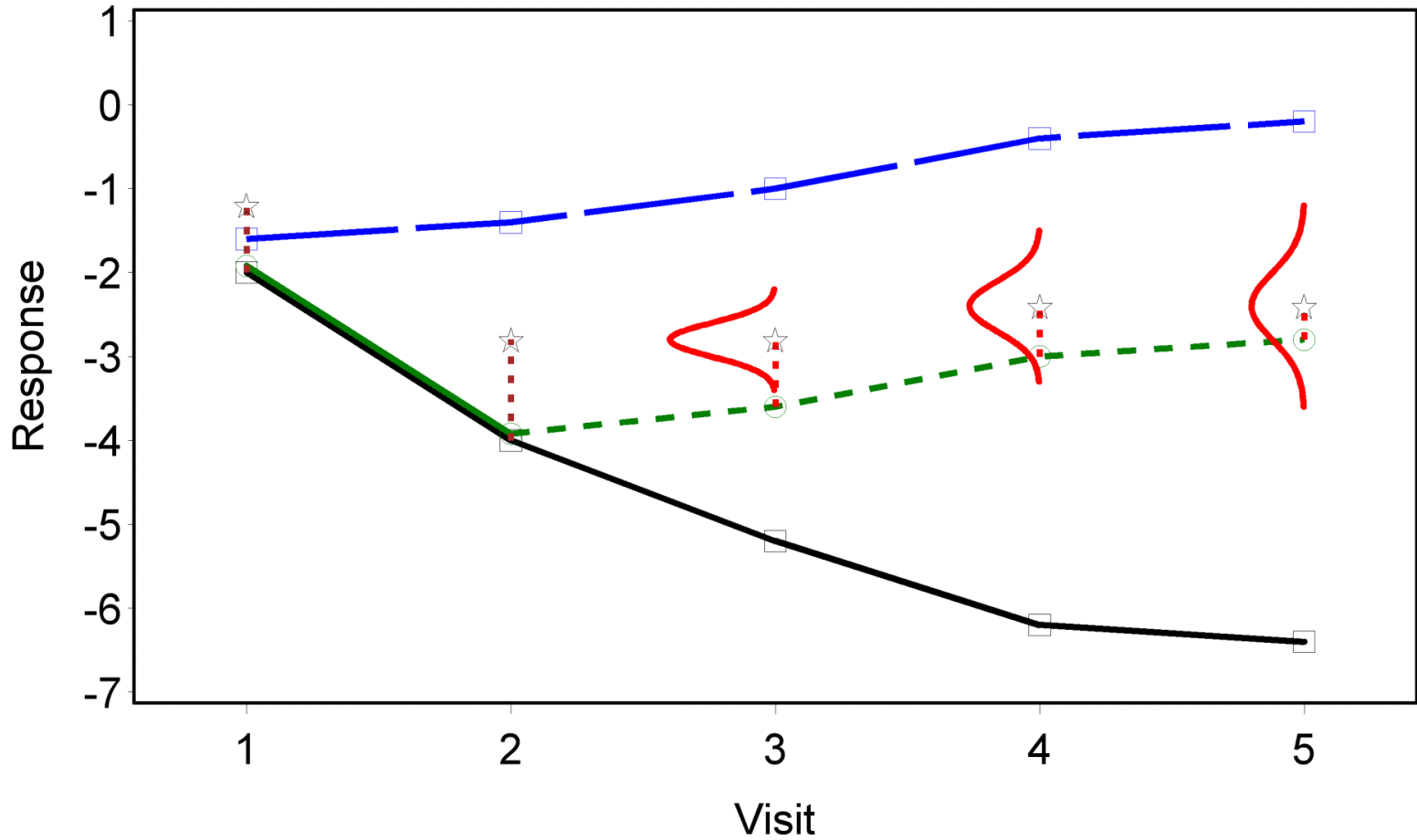
# Imputation assuming MAR. Withdrawal after two visits

## Plots from James Roger

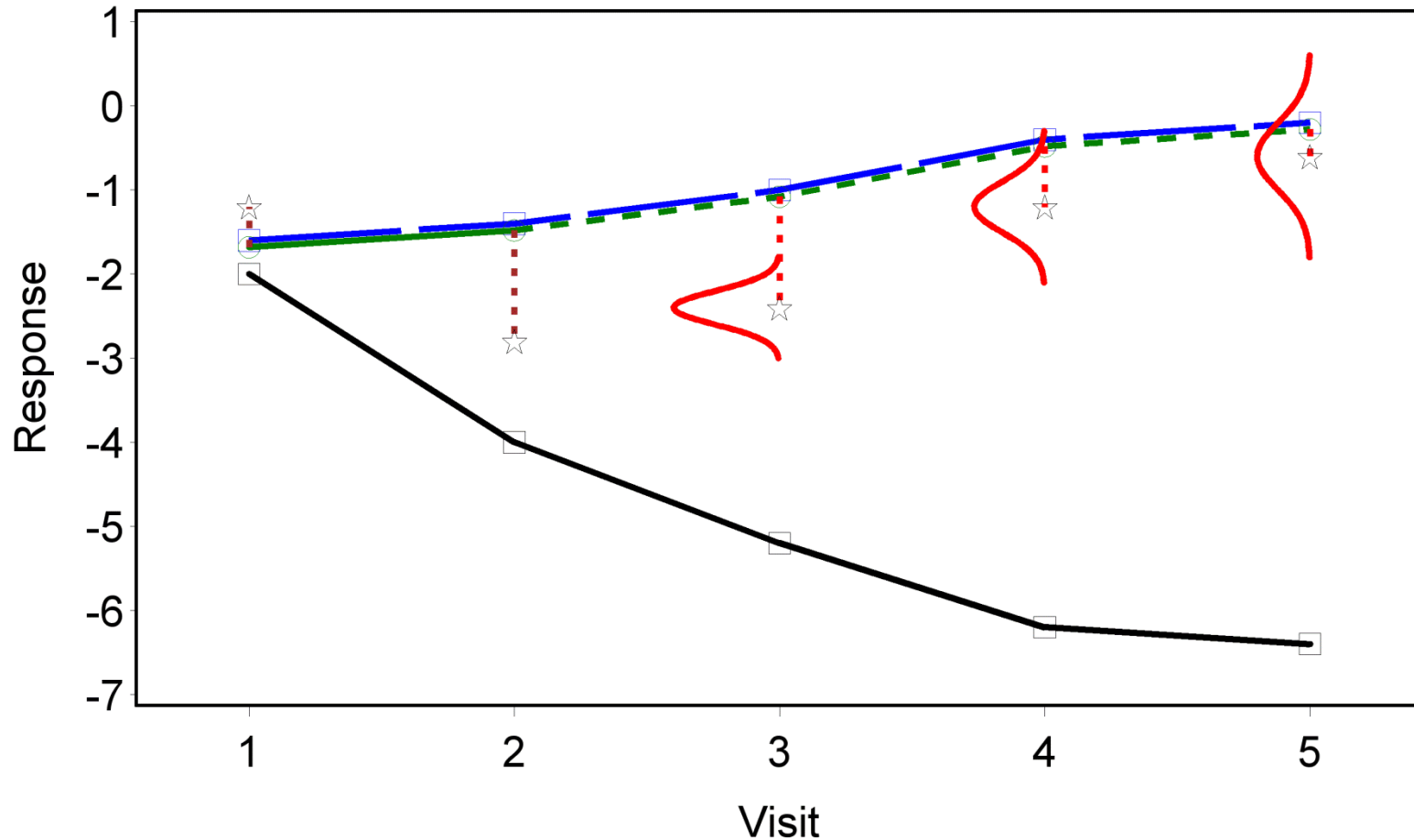


Black line Active. Blue line Reference. Dotted Green line (imputation).

# Copy Increment From Reference (CIR)

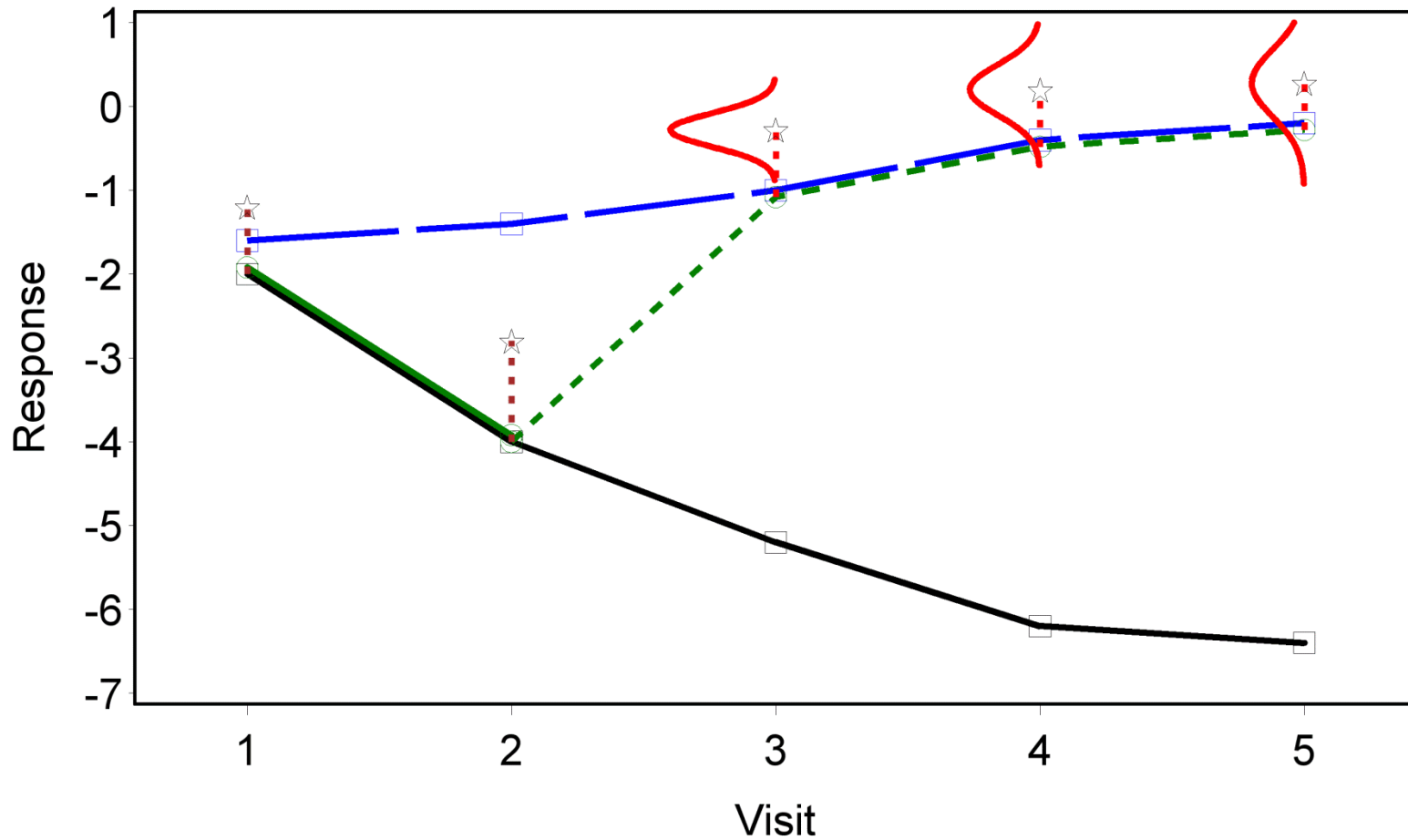


# Copy Reference (CR): Residuals prior to withdrawal are based on reference arm mean



Green line shows the means  $A_{JK}$  (circles), dotted after withdrawal.  
Brown residuals are for two observed values (star) before withdrawal.  
Red “residuals” show location of means (star) for conditional distribution.  
Red Normal curve indicates actual conditional distribution

# Jump to reference (J2R). Residuals based on deviation from assigned treatment arm



# Controlled Imputations: Delta Adjustment

- **Subtract a constant (delta) from imputed value at visit X that then further influences imputed values at visit  $> X$** 
  - **First missing visit only**
  - **All missing visits**
- **Subtract delta after completion of all imputations**
- **Progressively increase delta until conclusion from primary analysis is overturned**

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# Example Data from Major Depression

- **Two real but contrived data sets (n=100/arm)**
- **Drug arm patients randomly selected from 3 active arms**
- **Placebo arms mostly as is (with minor replication)**
- **Nearly identical designs**
  - **8-week, double blind, randomized 1:1:1:1**
  - **Assessments @ weeks 1,2,4,6,8**
  - **Similar inclusion / exclusion**
  - **Low dropout from EU study with ext and titration**
  - **High dropout from US fixed dose, no extension**



# Example Data

- **High dropout**
  - **Completion rates: placebo 60%, drug 70%**
  - **1000 planned observations, 850 available**
- **Low dropout**
  - **Completion rates: placebo 92%, drug 92%**
  - **1000 planned observations, 961 available**

**Therapeutic Innovation and Regulatory Science;**  
**2013, 48(1): 68-80.**

# Patient Retention

	Week				
	1	2	4	6	8
<b><u>High dropout</u></b>					
Placebo	8	7	12	13	60
Drug	9	6	10	5	70
<b><u>Low Dropout</u></b>					
Placebo	2	0	3	3	92
Drug	2	1	2	3	92

Prior to week 8 these values are the number of dropouts. For week 8 the values are the number of completers because week 8 is the last scheduled assessment.

# Example: Reference-Based Imputation Results

	LSMEANS		LSMEAN	Std	
	Placebo	Drug	Difference <sup>1</sup>	Error	P value
<b><i>High dropout (35%) dataset<sup>1</sup></i></b>					
<b>MAR</b>	<b>-5.95</b>	<b>-8.24</b>	<b>2.29</b>	<b>1.00</b>	<b>0.024</b>
<b>CIR</b>	<b>-5.95</b>	<b>-7.78</b>	<b>1.83</b>	<b>0.97</b>	<b>0.004</b>
<b>CR</b>	<b>-5.96</b>	<b>-7.71</b>	<b>1.75</b>	<b>0.98</b>	<b>0.075</b>
<b>J2R</b>	<b>-5.97</b>	<b>-7.57</b>	<b>1.60</b>	<b>0.99</b>	<b>0.110</b>
<b><i>Low dropout (8%) dataset<sup>1</sup></i></b>					
<b>MAR</b>	<b>-10.56</b>	<b>-12.40</b>	<b>1.84</b>	<b>0.70</b>	<b>0.009</b>
<b>CIR</b>	<b>-10.55</b>	<b>-12.27</b>	<b>1.72</b>	<b>0.70</b>	<b>0.015</b>
<b>CR</b>	<b>-10.55</b>	<b>-12.27</b>	<b>1.72</b>	<b>0.70</b>	<b>0.015</b>
<b>J2R</b>	<b>-10.55</b>	<b>-12.26</b>	<b>1.71</b>	<b>0.70</b>	<b>0.016</b>

Difference MAR vs. J2R over 6x greater in high dropout.

# Delta-adjustment Results

Value of Delta	<u>Low Dropout</u>			<u>High dropout</u>		
	Endpoint Contrast	Std Error	Pvalue	Endpoint Contrast	Std Error	PValue
0	1.85	0.71	0.009	2.31	1.02	0.024
<b>0.5</b>	1.77	0.71	0.013	2.00	1.03	<b>0.051</b>
2.0	1.52	0.73	0.037			
<b>2.5</b>	1.44	0.74	<b>0.051</b>			

- Delta required to overturn significance of primary result 5x larger for high dropout data set
- Change in endpoint contrast per 1 unit change in Delta
  - Low dropout = 0.16
  - High dropout = 0.62

# **Example: Specifying Sensitivity Analyses**

- **The key assumption made in the primary analysis regarding missing data is that the missingness arises from a missing at random mechanism. Sensitivity of inferences to this assumption will be evaluated by comparing the magnitude of the treatment effect from the primary analysis to...**

# Discussion

- Proper sensitivity analyses allow us to assess sensitivity
- Lower rates of dropout is the only way to improve sensitivity
- Controlled imputations are useful and intuitive
  - Assumptions can be informed by data obtained from follow-up phase

# Selected Publications

- A structured approach to choosing estimands and estimators in longitudinal clinical trials. (2012). *Pharmaceutical Statistics*; 11:456–461.
- Missing data: Turning guidance into action. (2013). *Statistics in Biopharmaceutical Research*; 5(4): 369-382.
- Recent Developments in the Prevention and Treatment of Missing data. (2013). *Therapeutic Innovation and Regulatory Science*; 48(1): 68-80.
- A structured framework for assessing sensitivity to missing data assumptions in longitudinal clinical trials. (2013). *Pharmaceutical Statistics*; 12:1–6.
- *Preventing and Treating Missing Data in Longitudinal Clinical Trials*. (2013). Cambridge University Press, Cambridge.
- Missing data in clinical trials: from clinical assumptions to statistical analysis using pattern mixture models. *Pharmaceutical Statistics*. (2013). DOI: 10.1002/pst.1549
- Analysis of longitudinal trials with missing data: a framework for relevant, accessible assumptions, and inference via multiple imputation. (2013). *Journal of Biopharmaceutical Statistics*, 23: 6, 1352-1371.
- *Clinical Trials with Missing Data: a Guide for Practitioners*. (2014) Wiley, Chichester.
- A Multiple-Imputation-Based Approach to Sensitivity Analyses and Effectiveness Assessments in Longitudinal Clinical Trials. (2014). *Journal of Biopharmaceutical Statistics*, 24: 211–228,



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