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# Adaptive Group Sequential Trials with Population Enrichment: Application to Cardiology

PhRMA Adaptive Working Group  
KOL Series  
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Cyrus R. Mehta, Ph.D  
Cytel Inc., Cambridge, MA

email: [mehta@cytel.com](mailto:mehta@cytel.com) – web: [www.cytel.com](http://www.cytel.com) – tel: 617-661-2011

# Acknowledgements

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- **We thank Stuart Pocock and Misha Salganik for helpful discussions**

# Population Enrichment Design for an Acute Coronary Syndrome Trial

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Major challenges to trial design for treatment of acute coronary symptoms include:

- low event rates
- tiny effect sizes
- diverse patient population

Such trials require enormous sample size commitments.

Therefore it is advisable to build in the possibility for adaptive changes to the design based on interim looks

# Case Study: Platelet Inhibition during Percutaneous Coronary Intervention

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- Composite primary endpoint – death, MI or ischemia driven revascularization **within 48 hours**
- Placebo event rate between 8% and 10%
- New drug expected to reduce placebo event rate by 20%
- But actual risk reduction could be as low as 15%

# Design Options Evaluated

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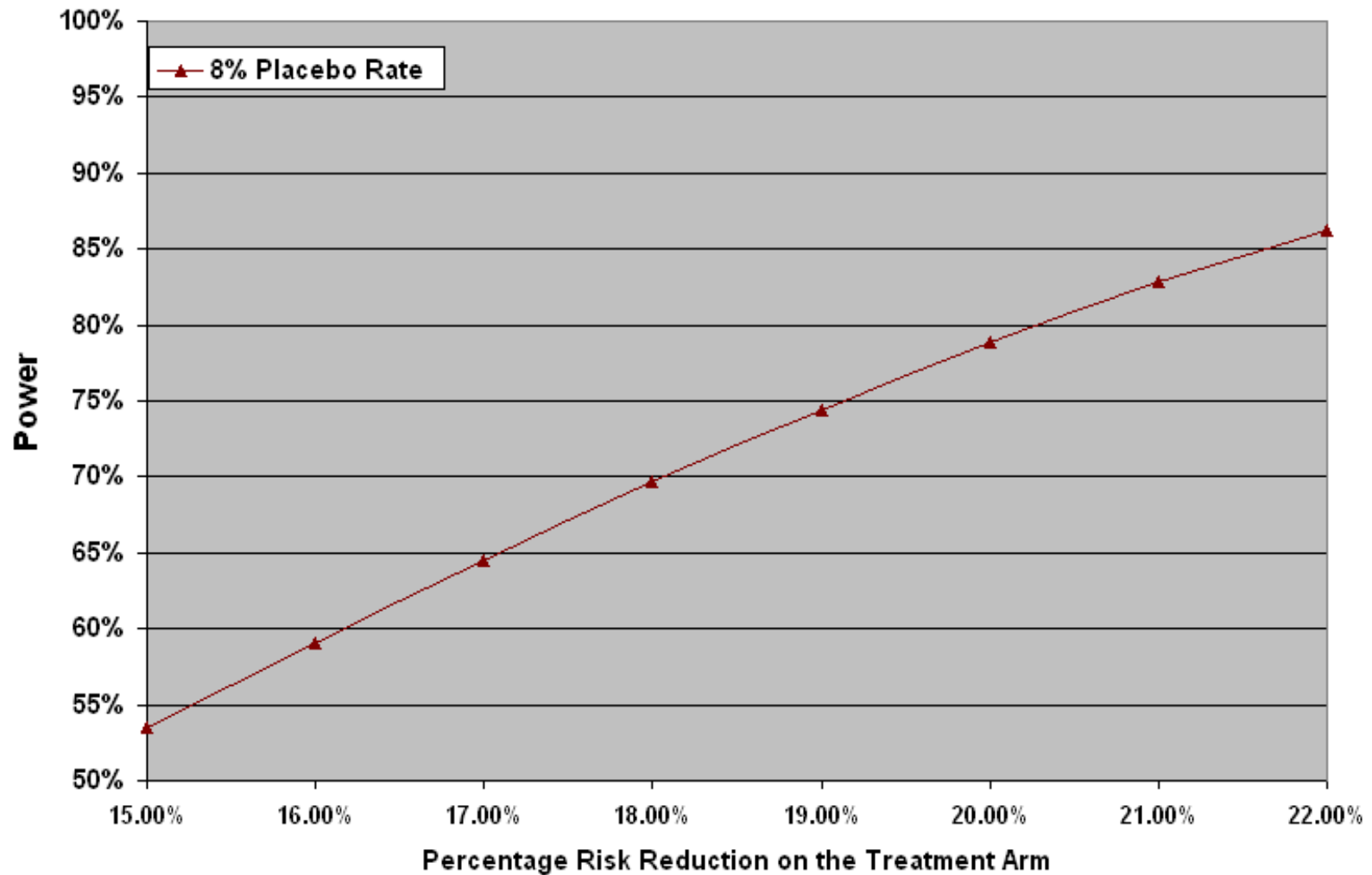
1. Fixed Sample Design
2. Group Sequential Design
3. Group Sequential Design with Sample Size Increase
4. Group Sequential Design with Sample Size Increase and Population Enrichment

# 1. Fixed Sample Design

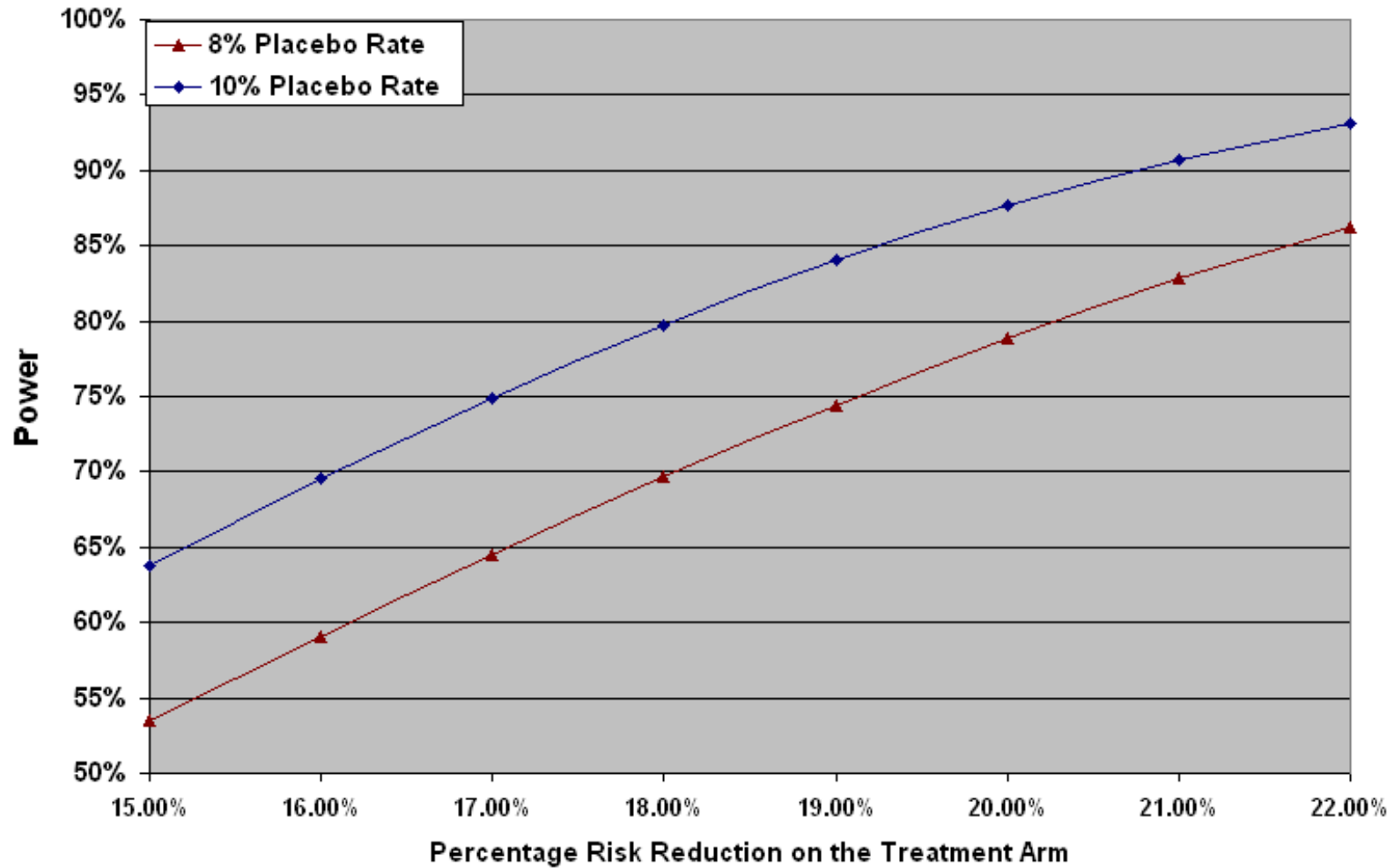
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- Sponsor decides on an initial commitment of  $N = 8000$
- This sample size provides more than 80% power if:  
    **risk reduction  $\geq 18\%$  and placebo event rate  $\geq 10\%$**
- If these parameter estimates were off by a few percentage points, study might be underpowered

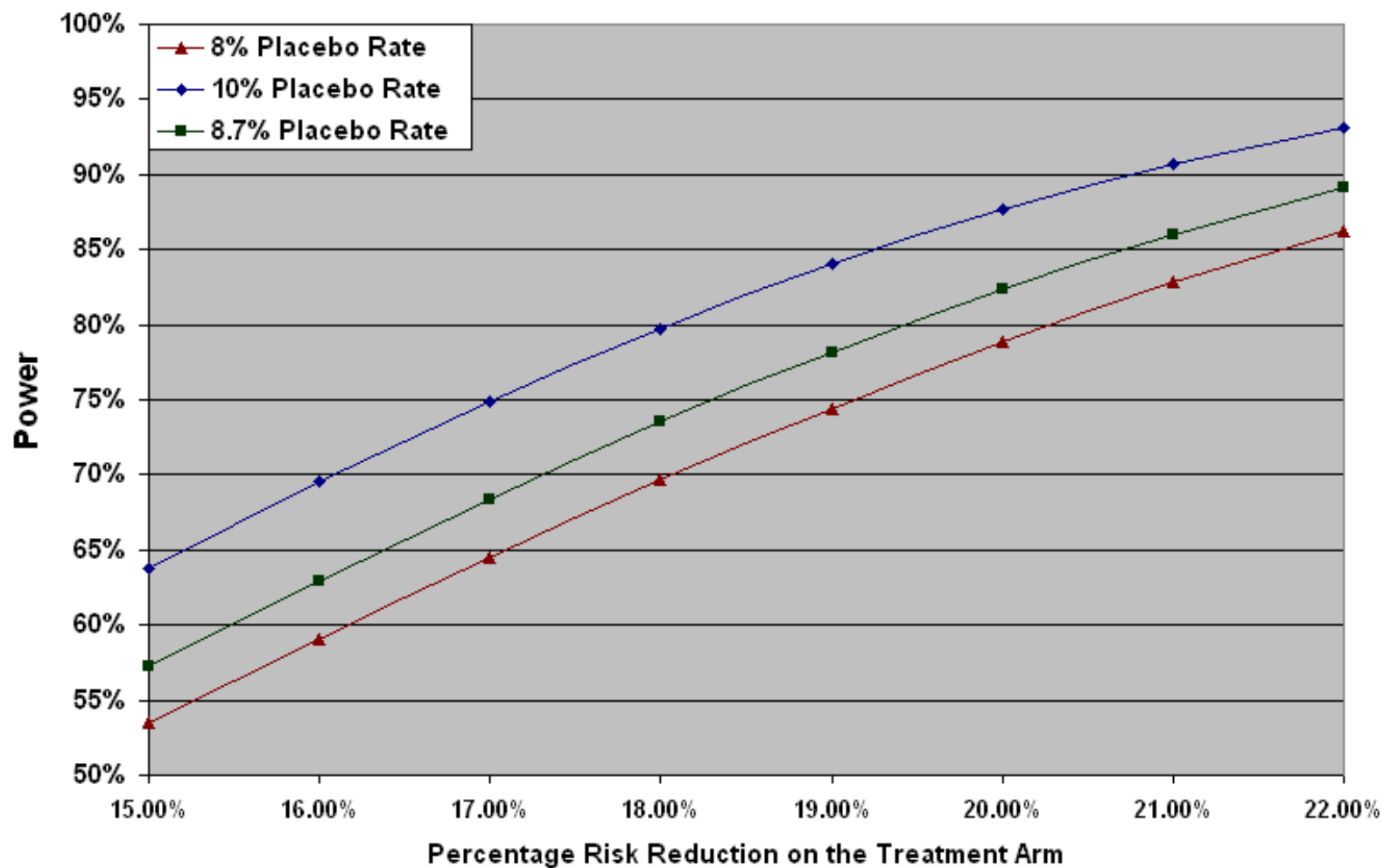
### Power Curves with Three Different Placebo Event Rates Fixed Sample Designs (N = 8000)



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# Can we do better?

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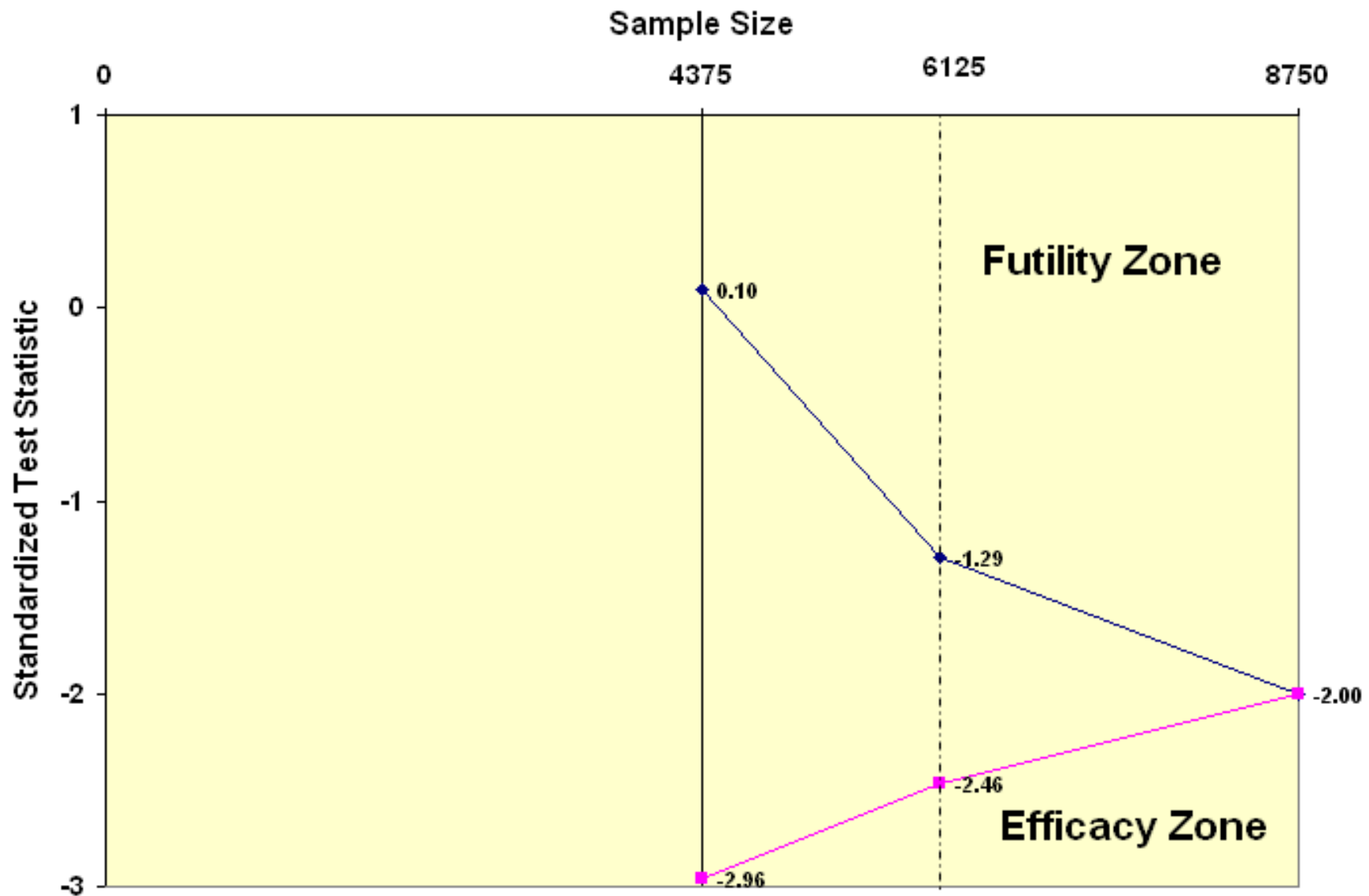
- 8000 patients is a very large fixed commitment
- We can do better with a group sequential design having early stopping boundaries for efficacy or futility
- Such a design would have a larger up-front commitment but lower expected sample size

## 2. Group Sequential Design (GSD)

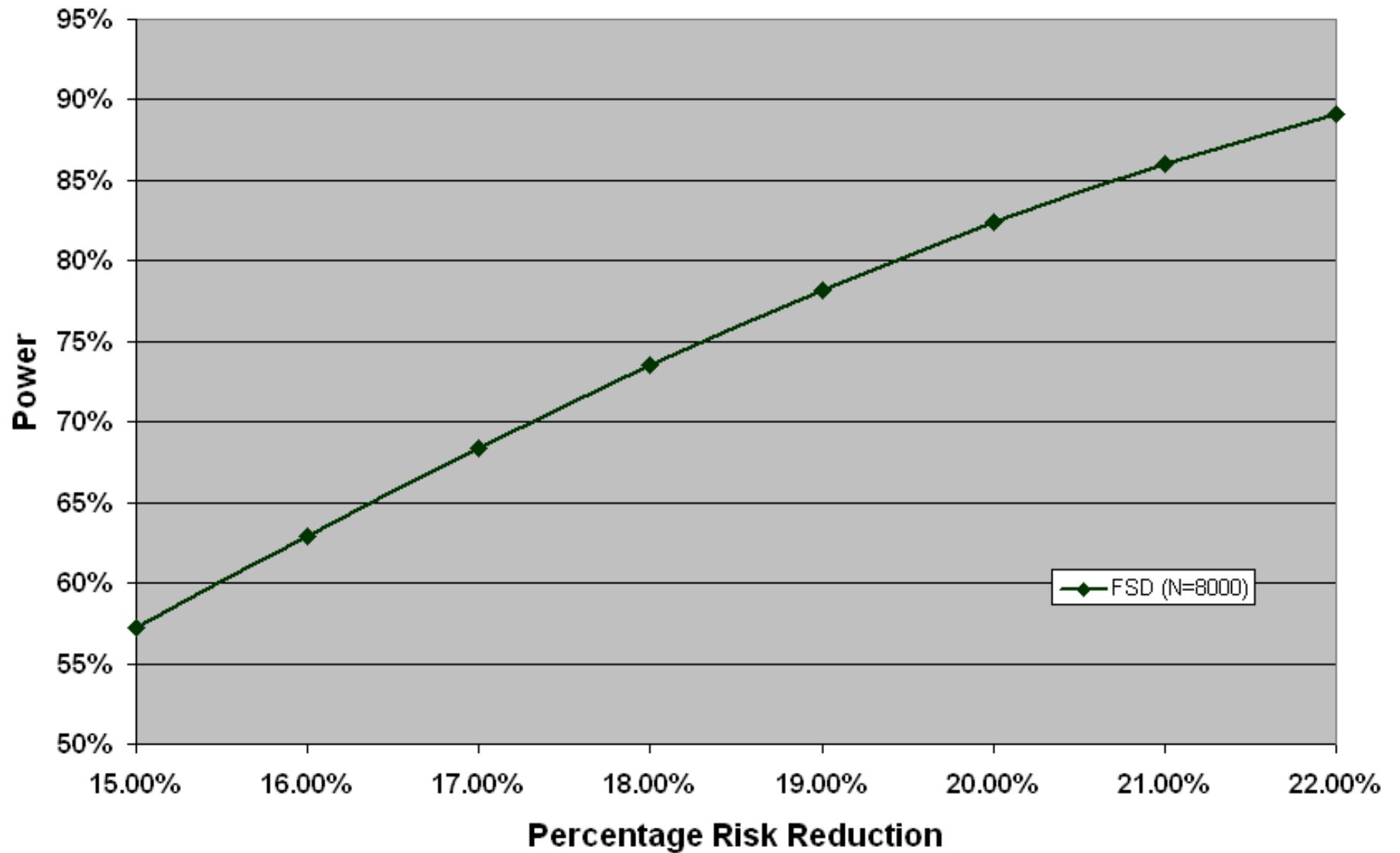
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- Enroll up to  $N_{\max} = 8750$  subjects
- First Interim Analysis (IA1): at 50% information
  - Stop for efficacy if  $Z \leq -2.9626$  (OBF bdry)
  - Stop for futility if 1% change in event rate **in the wrong direction**
- Second Interim Analysis (IA2): at 70% information
  - Stop for efficacy if  $Z \leq -2.4623$  (OBF bdry)
  - Stop for futility if conditional power  $\leq 20\%$

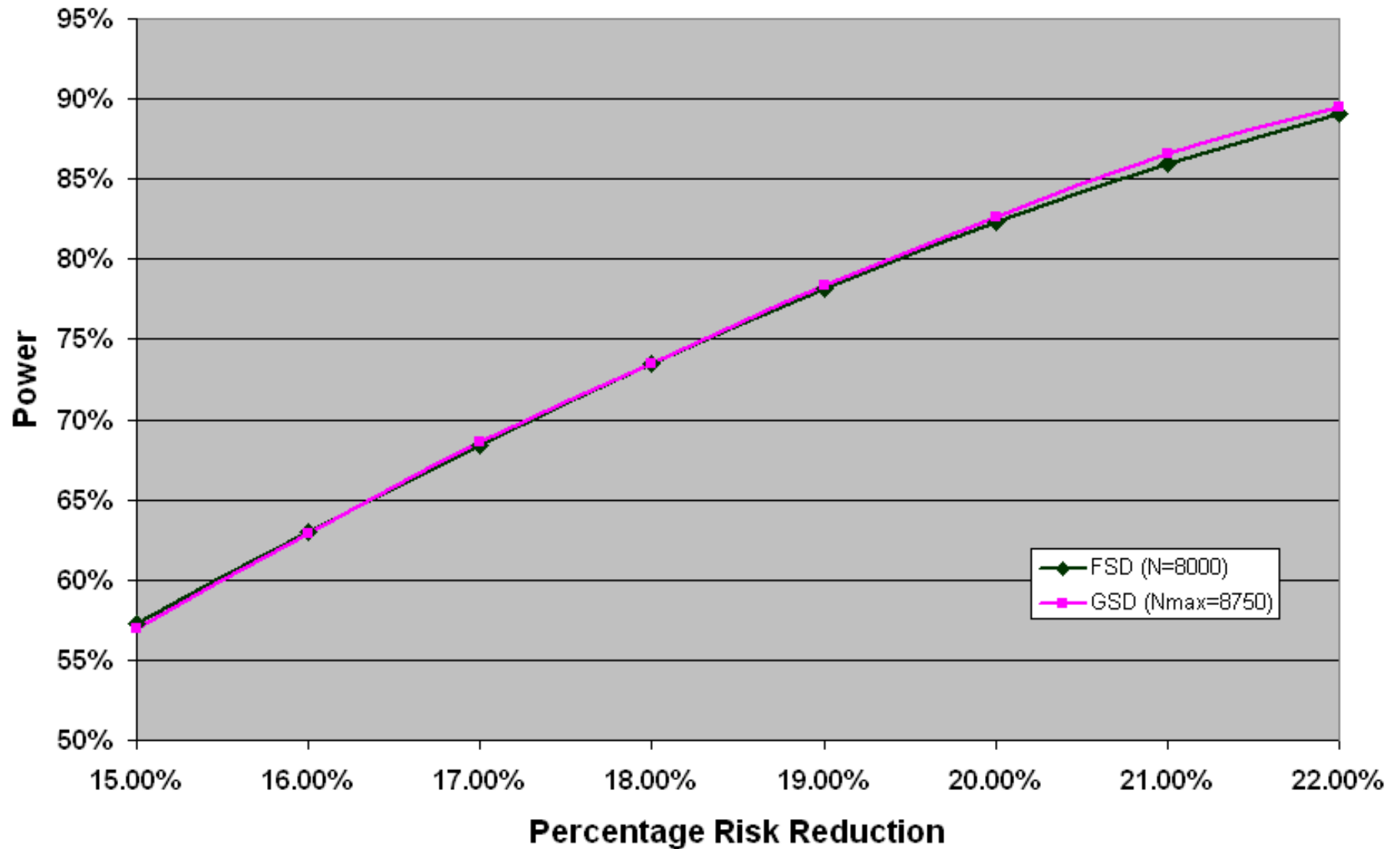
Group Sequential Design; 8750 Patients; Unconditional Type-1 Error is 0.025



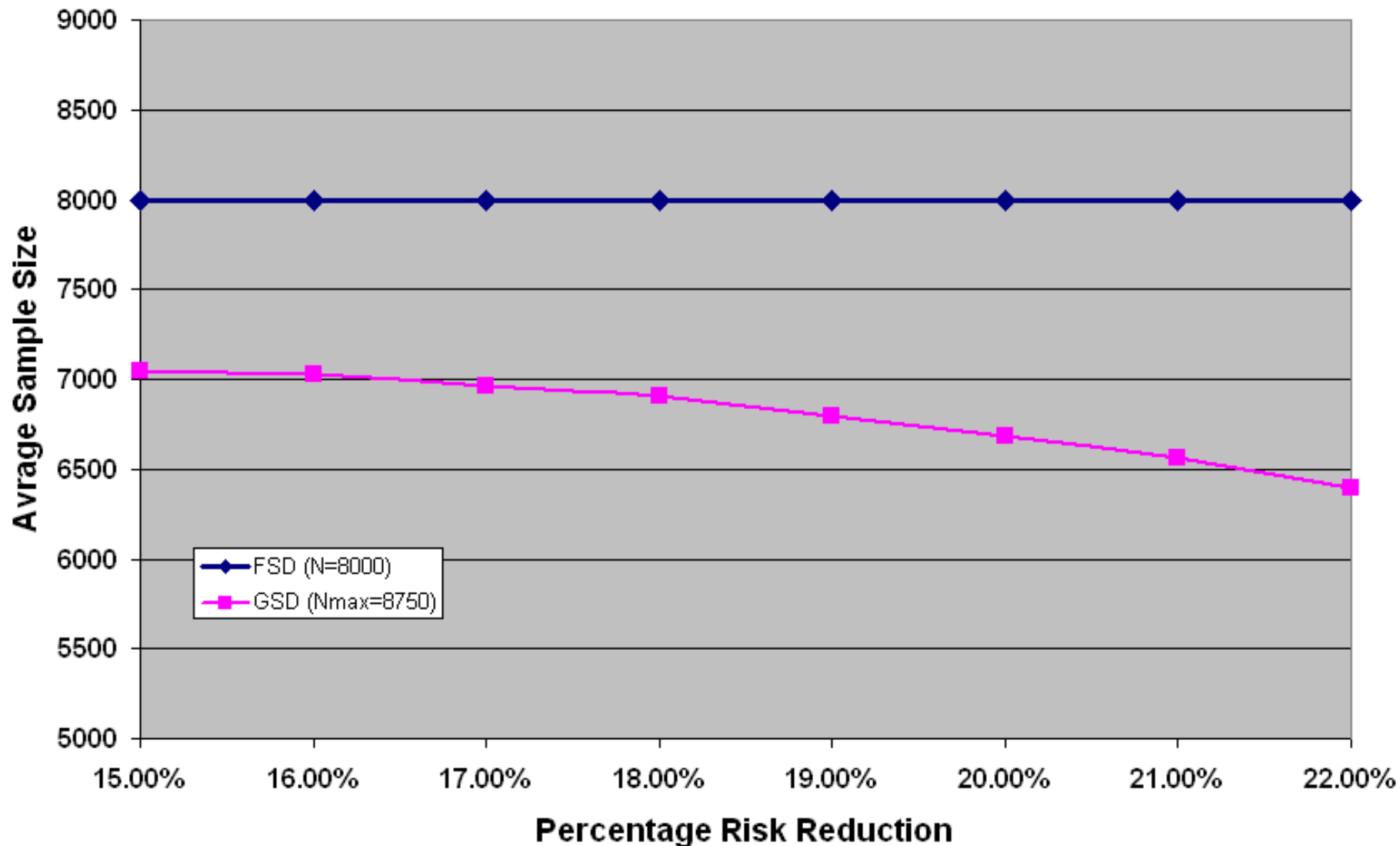
### Power Curve for Fixed-Sample Design



### Power Curves for Fixed-Sample and Group Sequential Designs



## Average Sample Sizes for Fixed Sample and Group Sequential Designs



# 3. GSD with Adaptive Sample Size Increase at IA2

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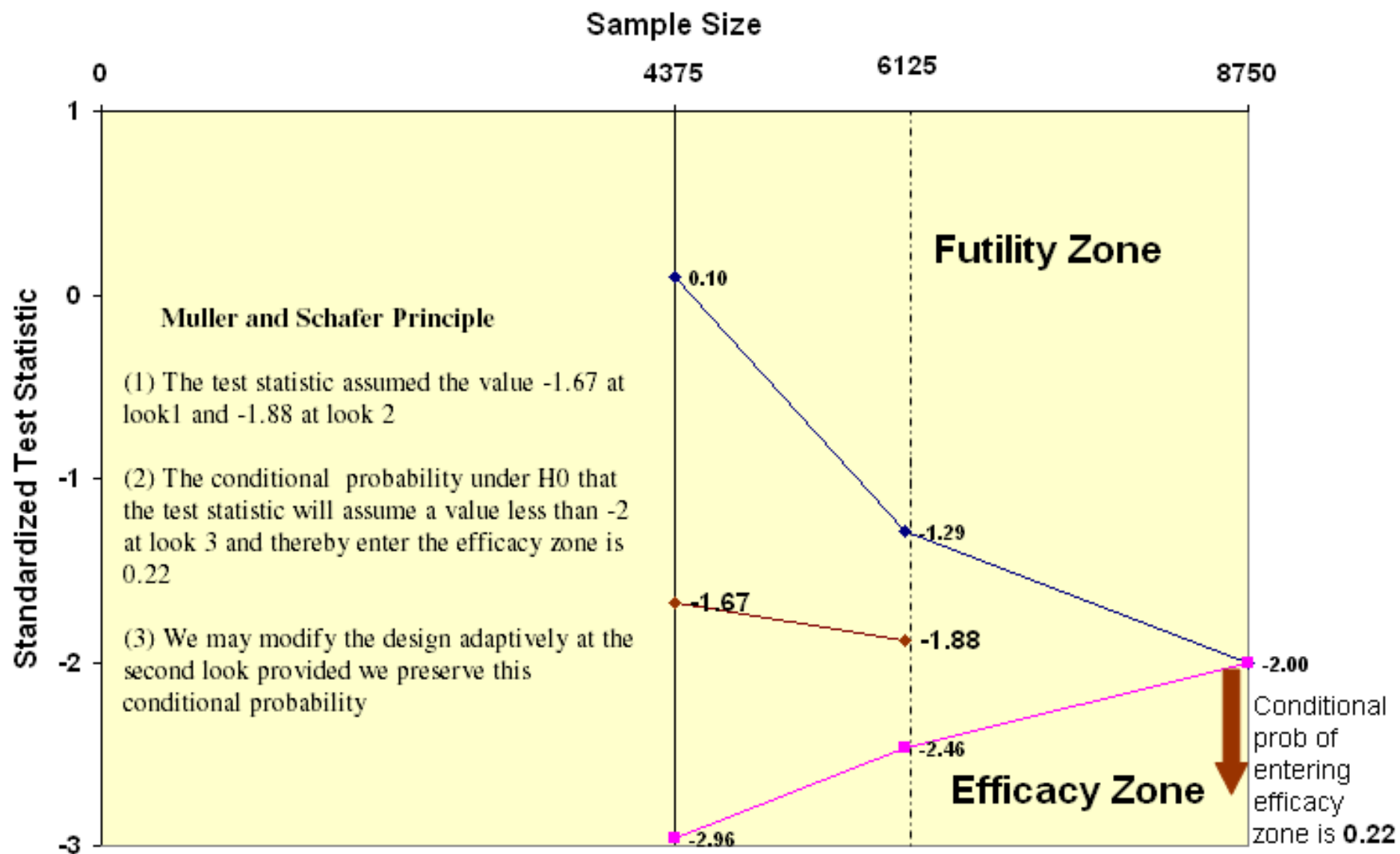
- Suppose neither efficacy nor futility boundaries are crossed at IA2
- Is conditional power less than 80%?
- If so, increase sample size such that conditional power equals 80%
- Subject to upper limit of 15,000 subjects

# Preservation of Type-1 Error after an Adaptive Design Change

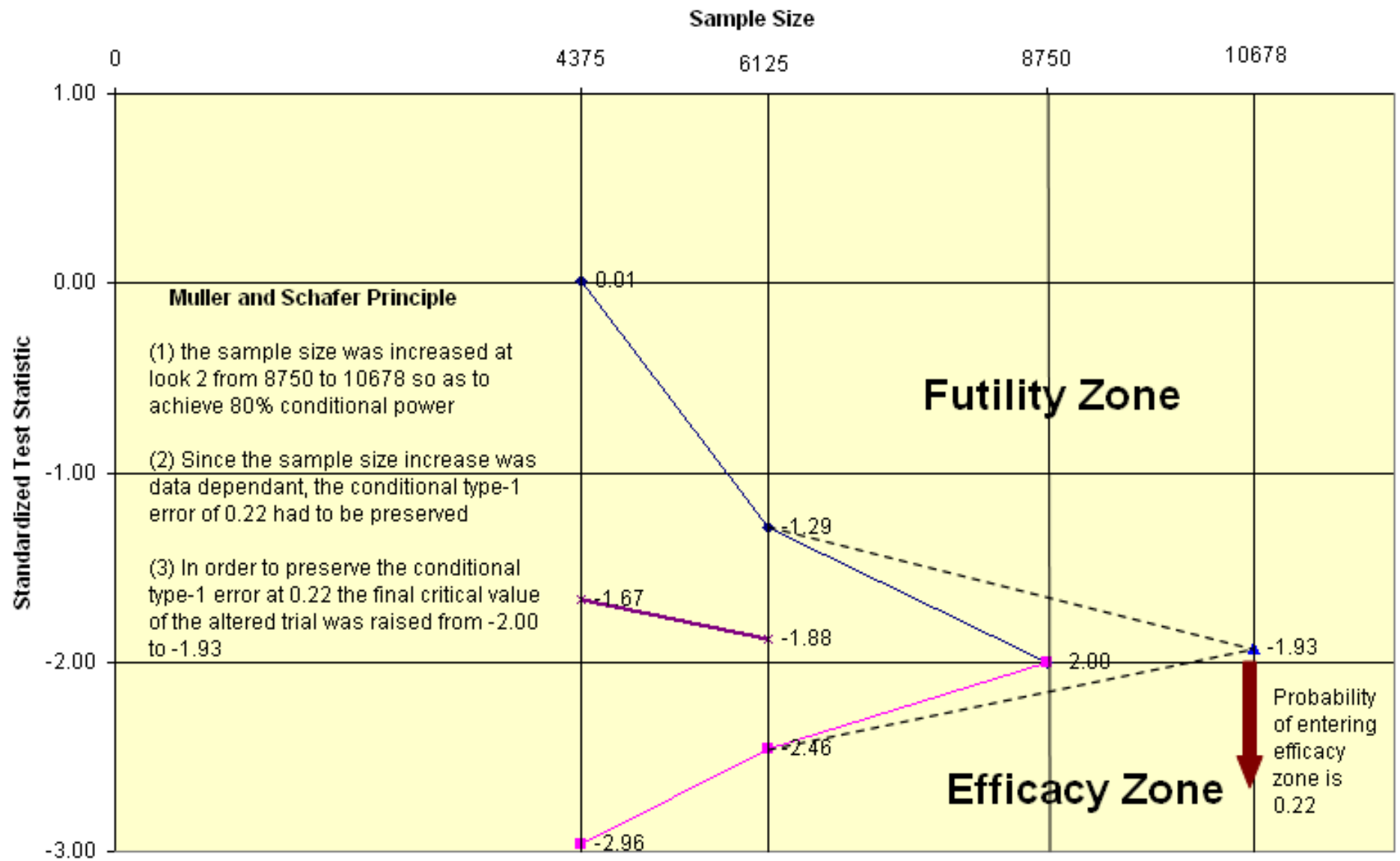
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- Unblinded sample size increase can inflate  $\alpha$
- To control this you must **preserve the conditional type-1 error** at the time of the adaptive change of design
- If you pre-specify that you will do this anytime you make an adaptive change, the overall type-1 error will still be  $\alpha$  (Muller and Schafer, 2001)
- Allowable adaptive changes include: **sample size change, change in number of future looks, change in future stopping boundaries, change in eligibility criteria**

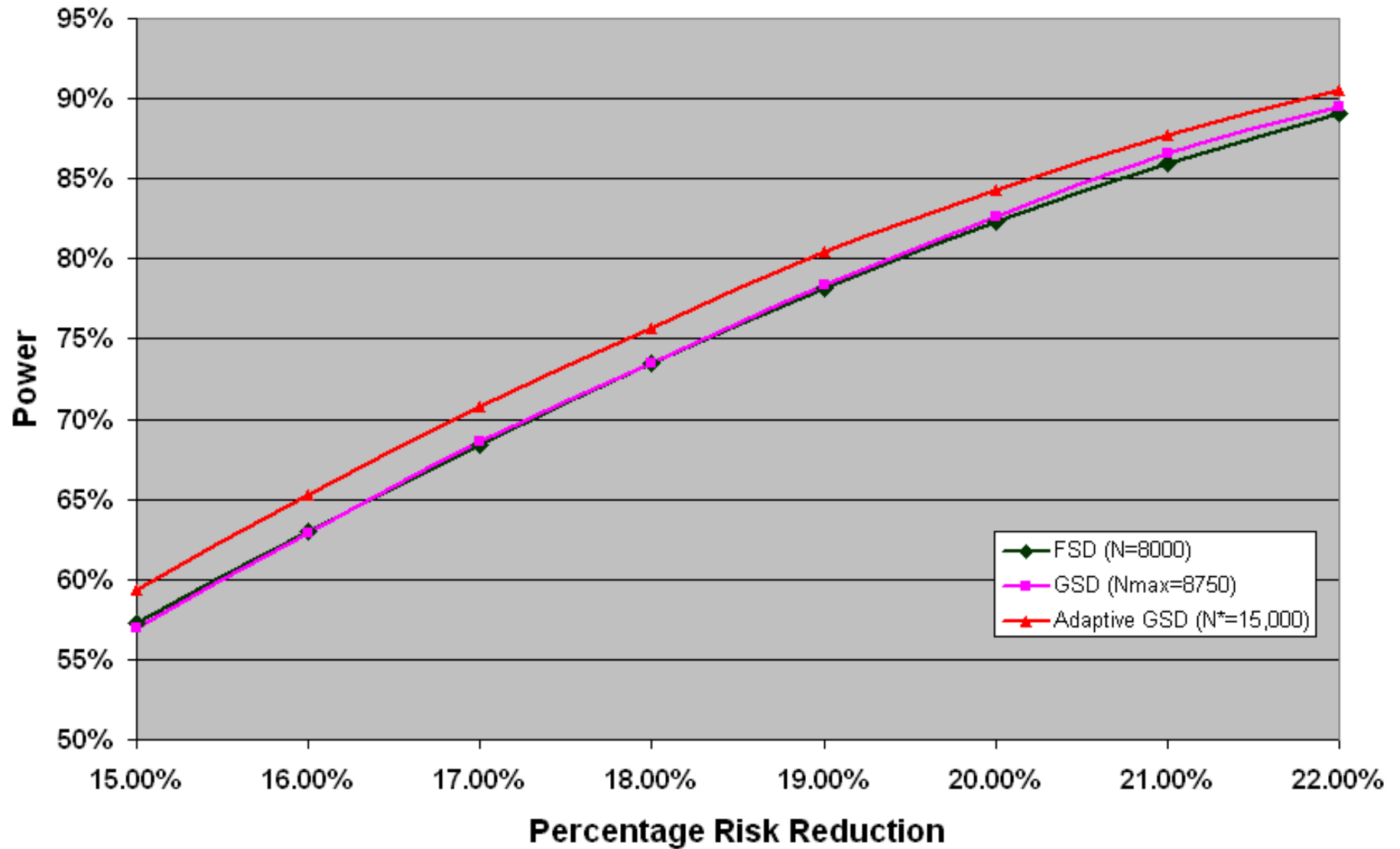
Group Sequential Design; 8750 Patients; Conditional Type-1 Error is 0.22



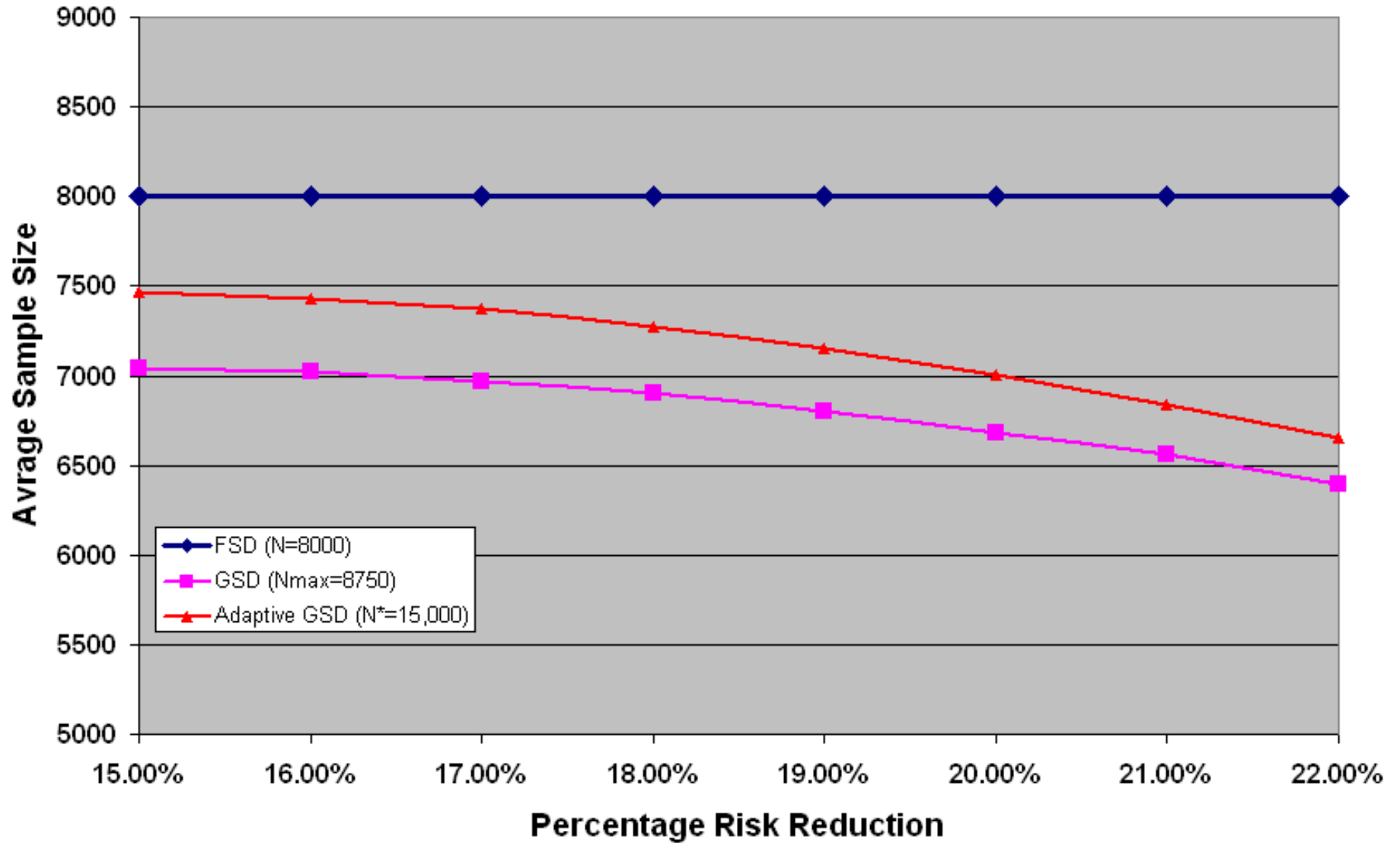
## Adaptive Sample Size Increase Keeping Conditional Type 1 Error Unchanged



Power Curves for Fixed-Sample, Group Sequential and Adaptive Group Sequential Designs



Average Sample Sizes for Fixed Sample, Group Sequential and Adaptive Group Sequential



# 4. GSD with Sample Size Increase and Population Enrichment

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- There is scientific evidence that some subgroups might benefit more than others from the new drug
- Sponsor wishes to take advantage of this possibility
- Design must allow drilling down into subgroups if overall benefit cannot be established

# Qualifications for Subgroups

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- Likely to influence the event rates
- More likely to influence experimental group than control group
- Easily identifiable in a clinical setting
- Consistently collected in the trial

# Prior Selection of Subgroup

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1. Using clinical judgement, create four **non-overlapping** partitions of the overall population

Non-Overlapping Partition	% of Population
high-risk and clopidogrel-naive	30%
high-risk and pre-treated with clopidogrel	30%
low-risk and clopidogrel-naive	20%
low-risk and pre-treated	20%

high risk patients are those with diabetes and a troponin + marker

**2. Form three nested subgroups from these four non-overlapping partitions:**

- $G_0$  = full population (100%)
- $G_1$  = high-risk subgroup (60% of  $G_0$ )
- $G_2$  = high-risk, clopidogrel-naive subgroup (50% of  $G_1$ )

**3. The goal is to try and win with  $G_0$ ; if not, then with  $G_1$ ; if not, then with  $G_2$**

# The Enrichment Strategy

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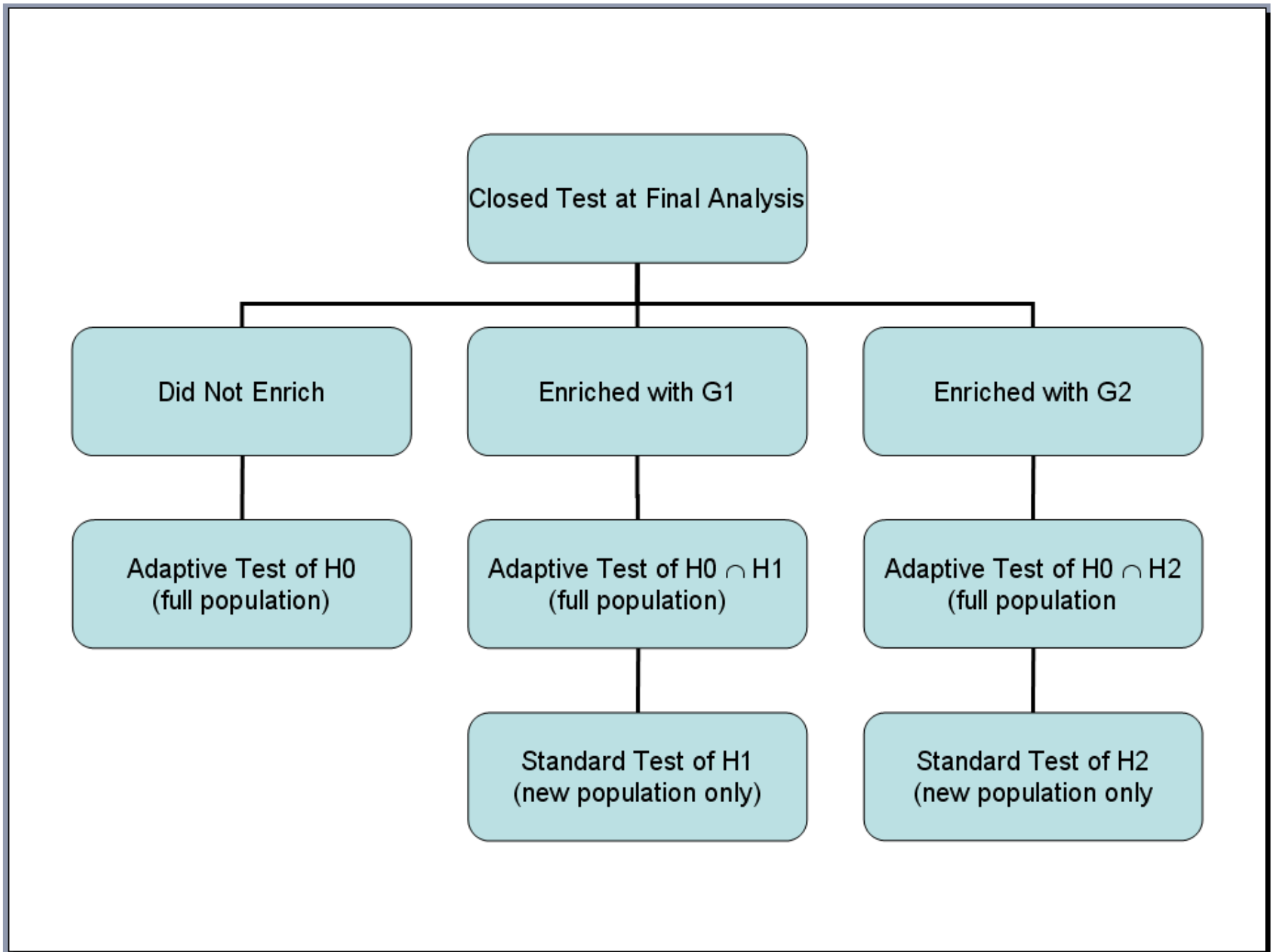
Suppose the group sequential boundary was not crossed at IA1 or IA2. Then:

- If  $CP \geq 80\%$  at IA2, carry on with no change
- If  $CP < 80\%$  at IA2:
  - Try for 80% with  $G_0$  and sample size increase
  - If unable, try for 80% CP by enriching with only  $G_1$  patients and sample size increase
  - If unable, try for 80% CP by enriching with only  $G_2$  patients and sample size increase
- Terminate for futility if  $CP < 20\%$  despite enrichment and sample size increase

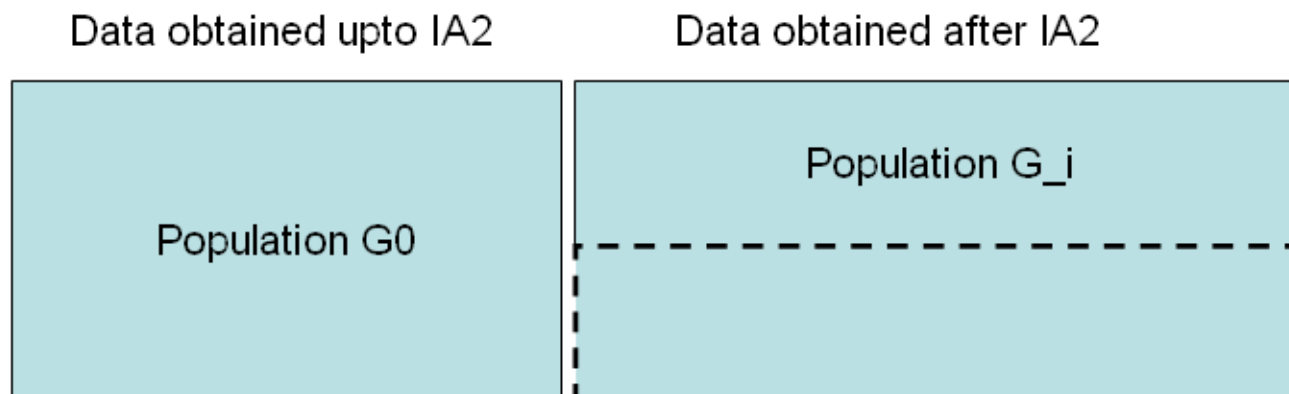
# Hypothesis Testing Strategy

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- For populations  $\{G_1, G_2, G_3\}$ , let  $\{H_1, H_2, H_3\}$  be corresponding null hypotheses that treatment and control event rates are equal
- Consider three cases:
  - Case 1 if population was not enriched, test  $H_0$  at final analysis
  - Case 2: if population was enriched by  $G_1$ , test  $H_1$  at final analysis
  - Case 3: population was enriched by  $G_2$ , test  $H_2$  at final analysis
- The testing strategy must ensure **strong control** of type-1 error. This means that **no matter which hypothesis is tested, the false positive rate must not exceed  $\alpha$**



# Graphical Depiction of Hierarchical Testing



- **Test 1** is performed with combined data from G0 and G<sub>j</sub>
- If G<sub>j</sub> is also G0 (i.e., no enrichment), no further testing
- If G<sub>j</sub> is either G1 or G2 (i.e., enrichment) perform **Test 2**
  - **Test 2** is only performed with the new data obtained after IA2

# Proof that Test Procedure is Closed

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$$H_0 \cap H_1 \cap H_2$$

$$H_0 \cap H_1$$

$$H_0 \cap H_2$$

$$H_1 \cap H_2$$

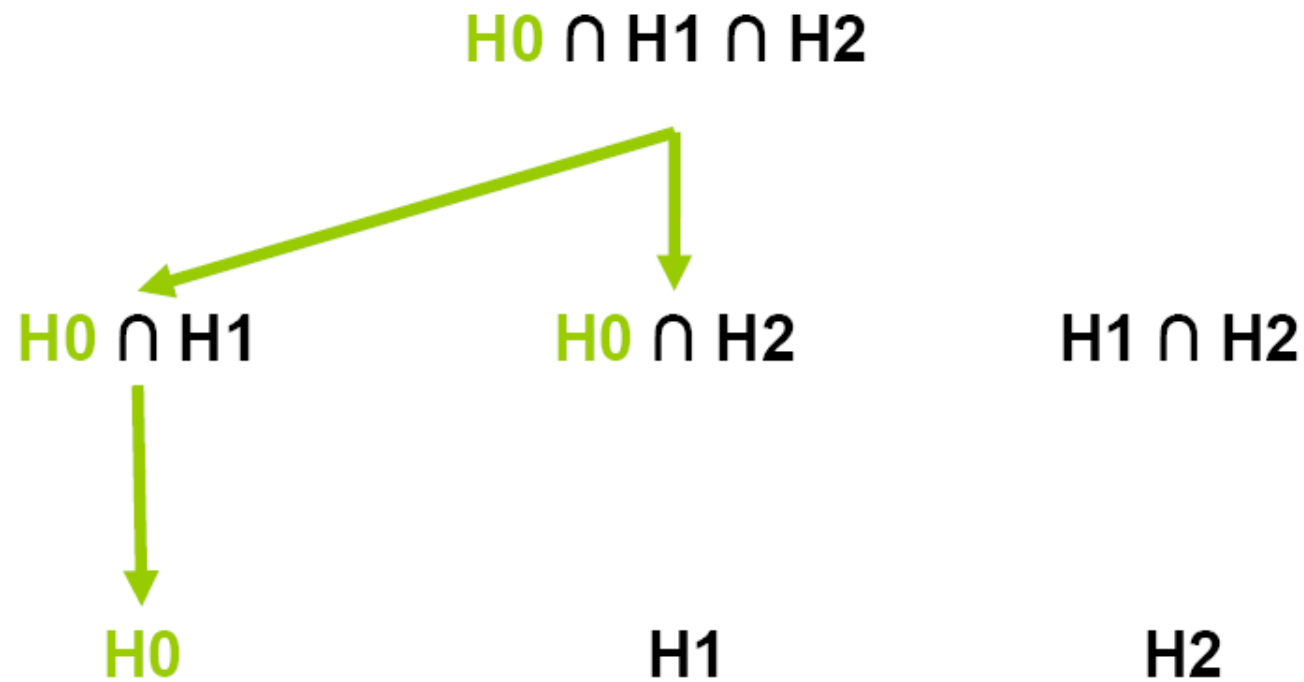
$$H_0$$

$$H_1$$

$$H_2$$

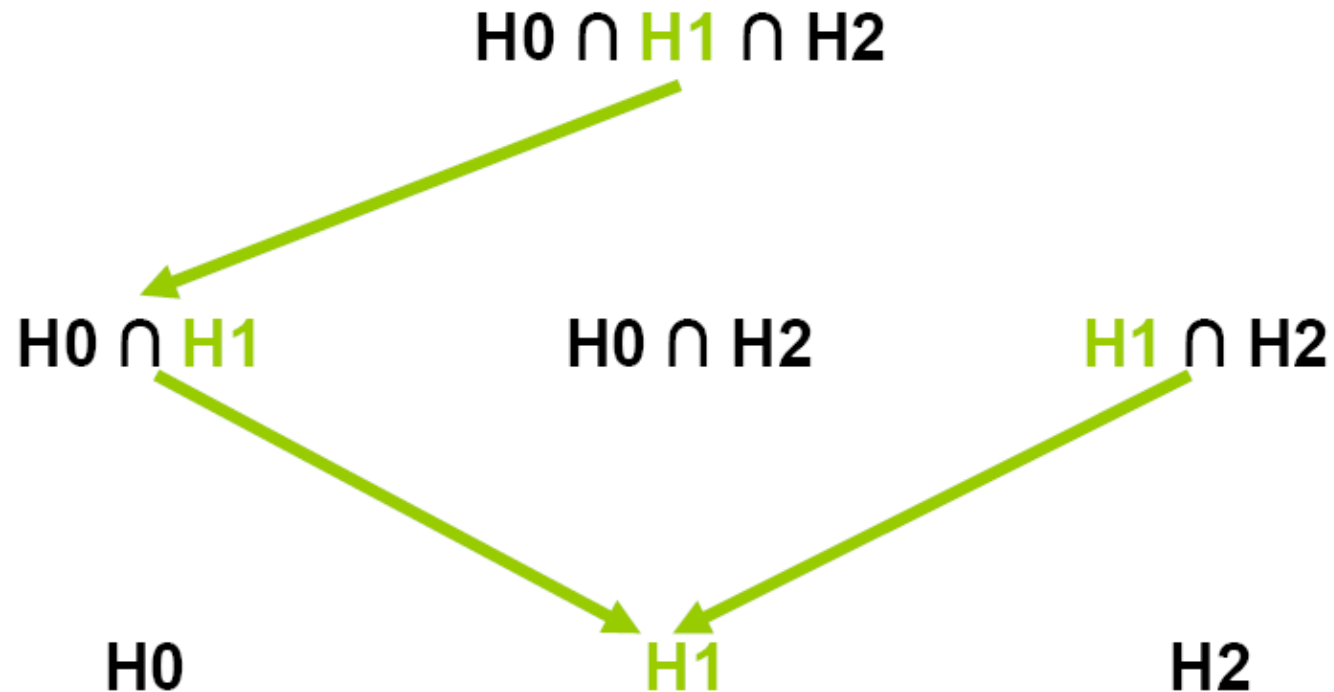
To reject any hypothesis you must also reject all intersections of that hypothesis with all other hypotheses

**Case 1:** If you don't enrich, all these tests must be rejected in order to claim G0



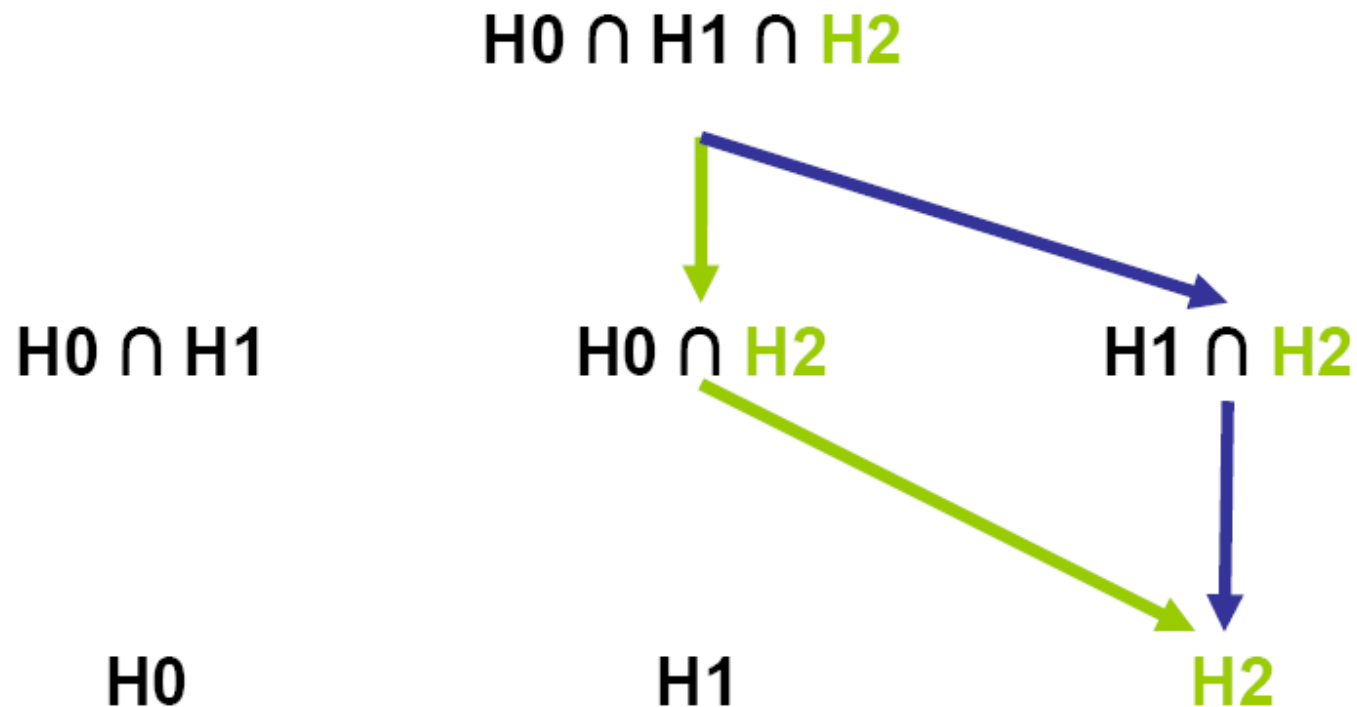
If you don't enrich, you must reject  $H_0$  at level-alpha in order to win with  $G_0$ . Test 1 (on the total population) is an adaptive level-alpha test of  $H_0$ . If it rejects, all the other tests indicated automatically reject also at level-alpha.

## Case 2: If you enrich with G1, all these tests must be rejected to claim G1



If you enrich with G1 you must first reject  $(H_0 \cap H_1)$  with Test 1, the “gatekeeper”. This is a level-alpha adaptive test. Then you must reject  $H_1$  with Test 2 using only the new G1 data. This is a conventional level-alpha test. If it rejects, all other tests indicated reject automatically at level-alpha

# Case 3: If you enrich with G2, all these tests must be rejected to claim G2



If you enrich with G2 you must first reject  $(H_0 \cap H_2)$  with Test 1, the “gatekeeper”. This is a level-alpha adaptive test. Then you must reject H2 with Test 2 using only the new G2 data. This is a conventional level-alpha test. If it rejects all other tests indicated automatically reject at level-alpha

# Properties of Testing Strategy

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- **Closed test!**. Guarantees strong control of type-1 error; i.e., chance of false rejection of either  $H_0$  or  $H_1$  or  $H_2$  cannot exceed  $\alpha$
- Boosts power by 2-5% if new treatment benefits all subgroups homogeneously
- Boosts power by 7-18% if new treatment benefits  $G_1$  or  $G_2$  differentially relative to  $G_0$

# Verify by Simulation

## Simulations for TheXYZ Company

### Population

Parameters of Atomic Subgroups

Parameter	HighR + Naïve	HighR + PreTrt	LowR + Naïve	LowR + PreTrt	
Subgr. Fr.	0.30	0.30	0.20	0.20	0.087
$\pi_c$	0.120	0.090	0.070	0.050	
$\pi_t$	0.084	0.072	0.063	0.048	
% Improvement	30.0%	20.0%	10.0%	4.0%	

Subpopulations of interest

Refresh

Subpop.	Subpop. Fraction	Event Rates		% Improv.	Difference $\delta$	Discount Factor
		$\pi_c$	$\pi_t$			
G <sub>0</sub>	1.00	0.087	0.069	20.7%	0.018	1.00
G <sub>1</sub>	0.60	0.105	0.078	25.7%	0.027	1.00
G <sub>2</sub>	0.30	0.120	0.084	30.0%	0.036	1.00

G<sub>0</sub>: All Patients, G<sub>1</sub>: HighR Patients, G<sub>2</sub>: HighR & Plavix Naïve Patients

Total Number of Simulations	10000
Initial Random Number Seed	clock

Run

Stop

Reset

### Test

Type-I Error ( $\alpha$ )	0.025
Initial Total Sample Size (Both Arms; $n_{max}$ )	8000

Look #	SS (Both Arms)	Stopping Rule	
		Efficacy	Futility
1	4000	Z $\geq$ 2.9626	% Impr. < -1%
2	5600	Z $\geq$ 2.4623	CP < 0.2
3	8000	Z $\geq$ 2.0018	

### Adaptation

Max. Sample Size With Adaptation (Both Arms; $n^*_{max}$ )	15000
Adaptation Criterion: CP $\geq$ Upper Threshold	0.8

Approach to Sample Size Re-estimation

Single Trial

Separate Trials

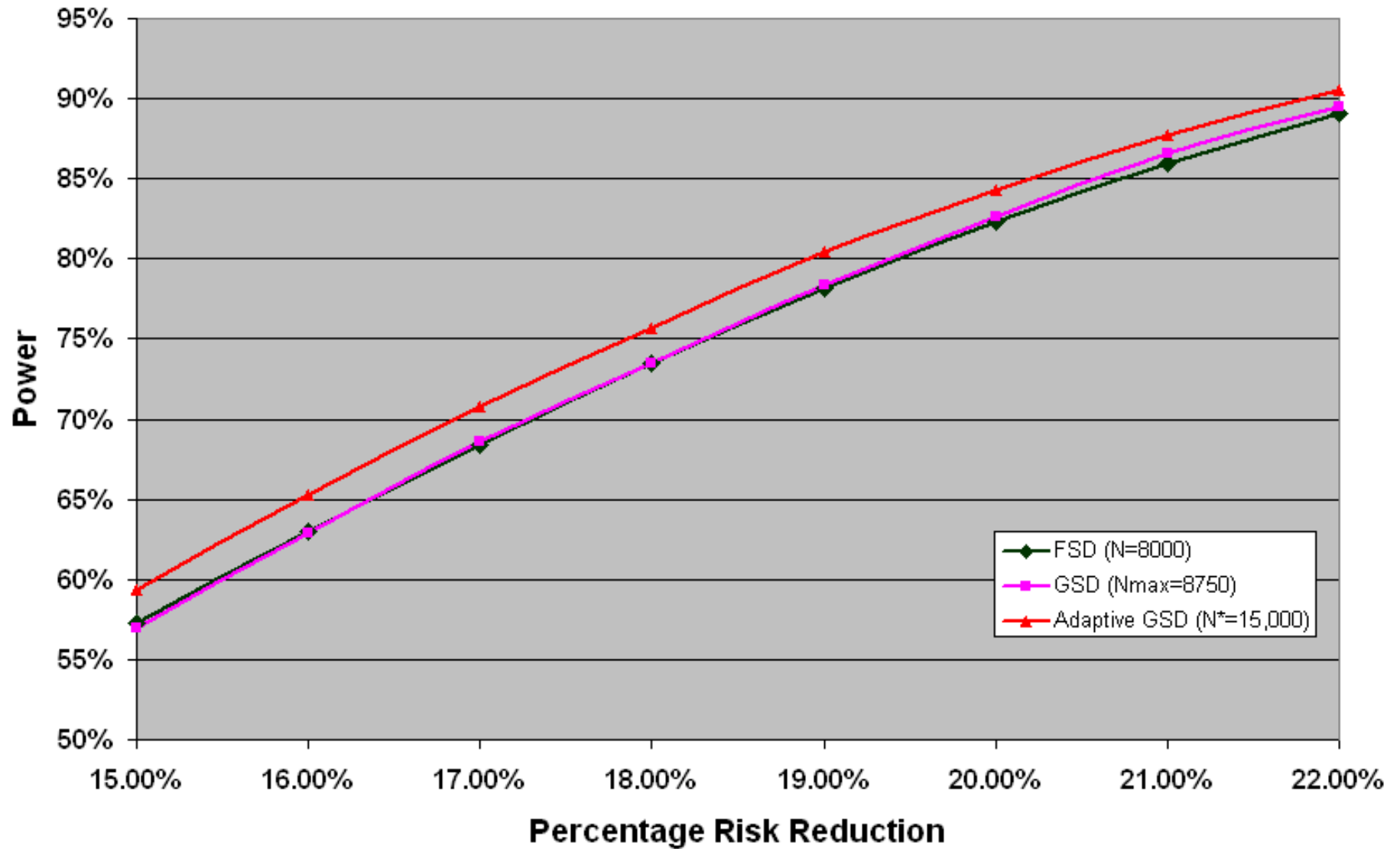
Disable Enrichment

Compute Power with Fixed Sample Size (Both Arms)

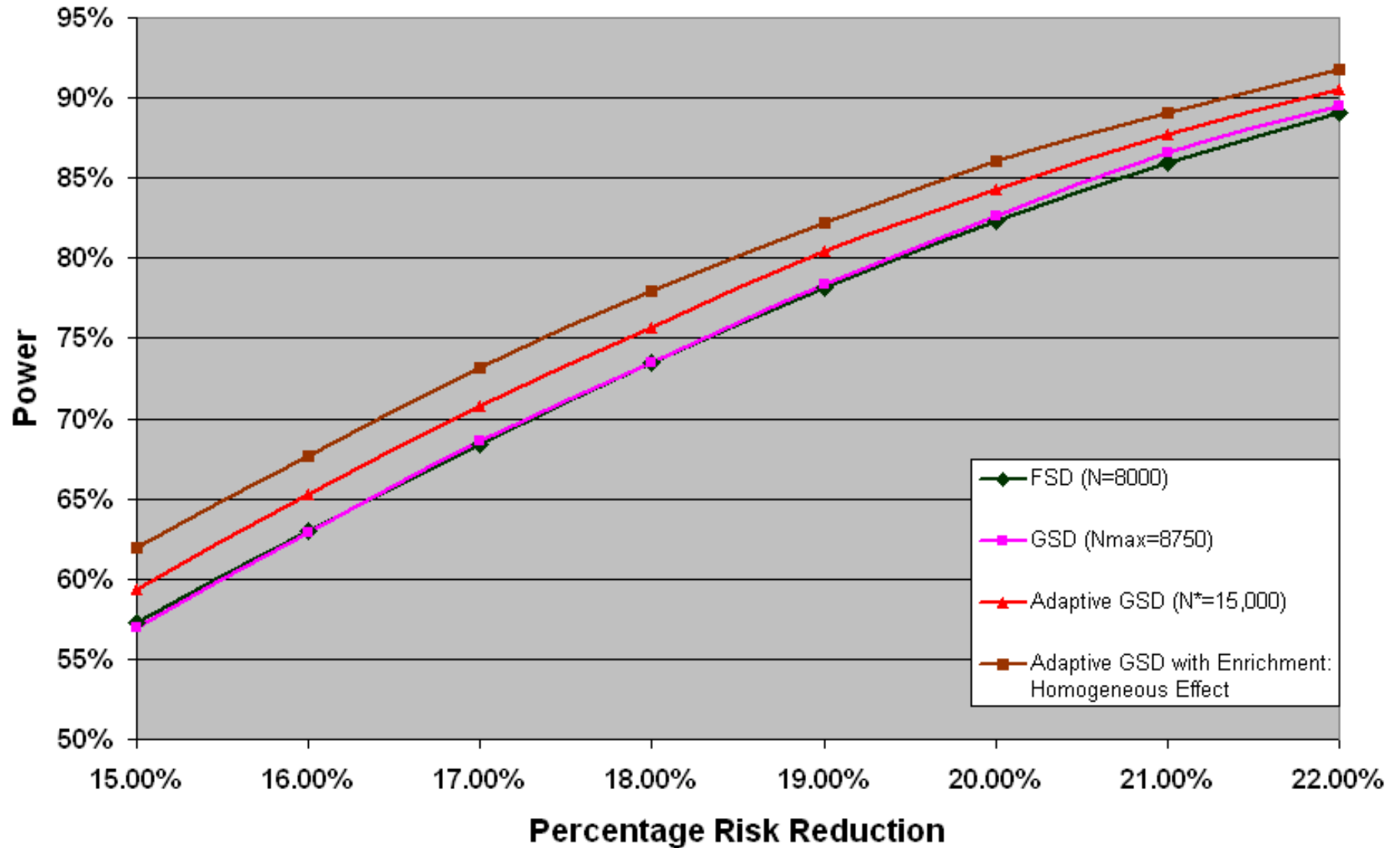
$n_{max}$

$n^*_{max}$

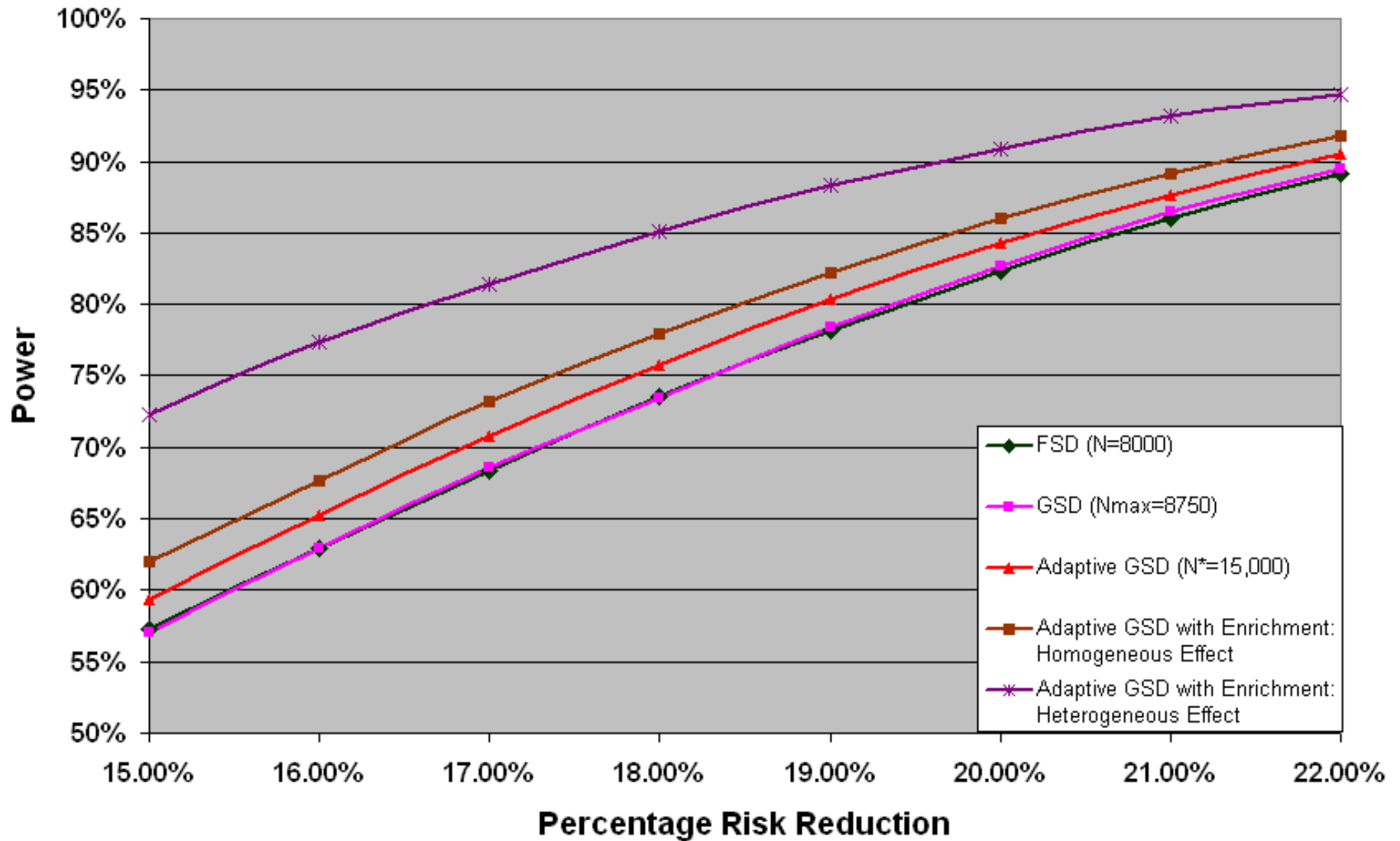
Power Curves for Fixed-Sample, Group Sequential and Adaptive Group Sequential Designs



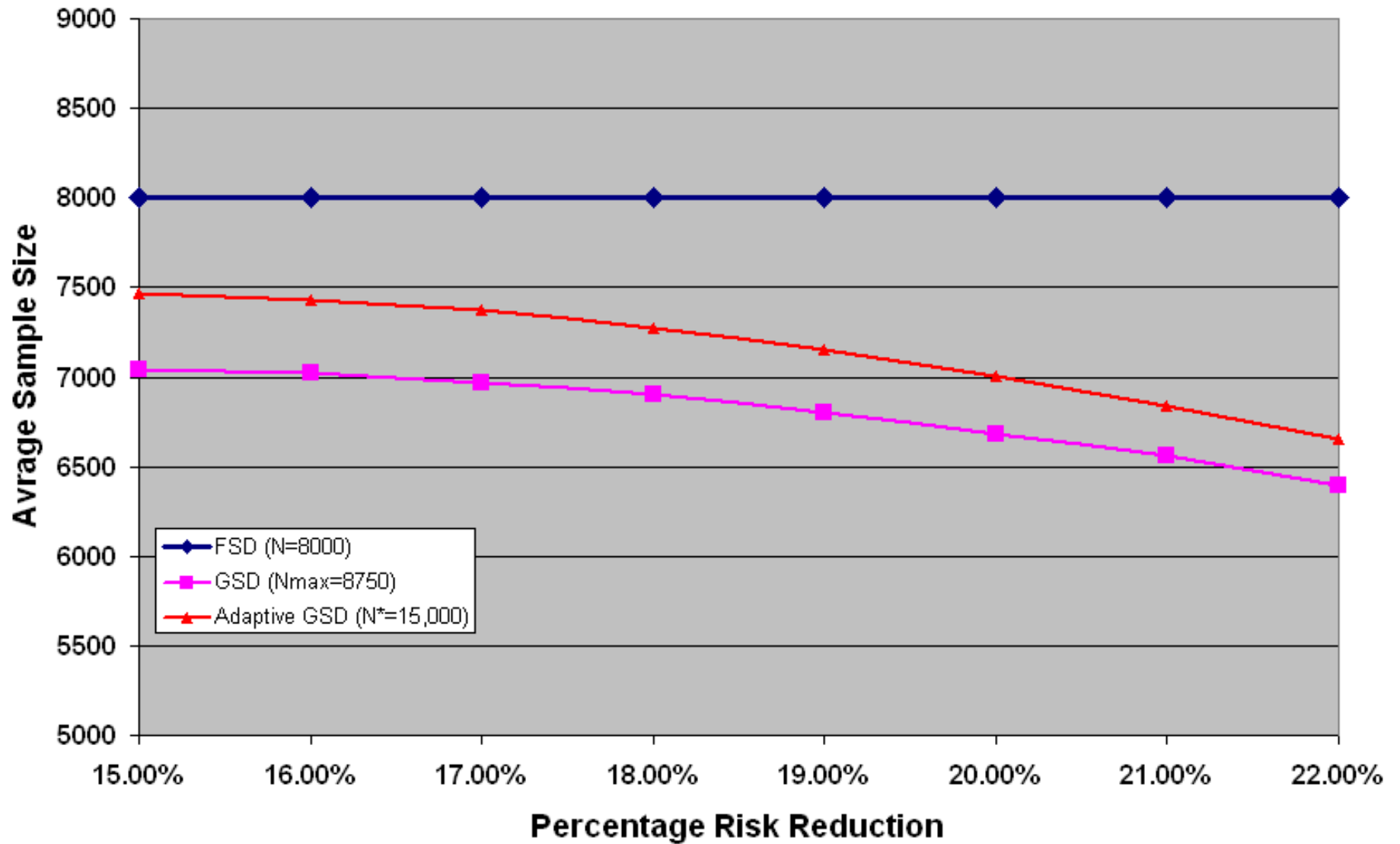
### Power Curves for Fixed-Sample, Group Sequential, Group Sequential Adaptive and Enrichment under Homogeneous Treatment Effect



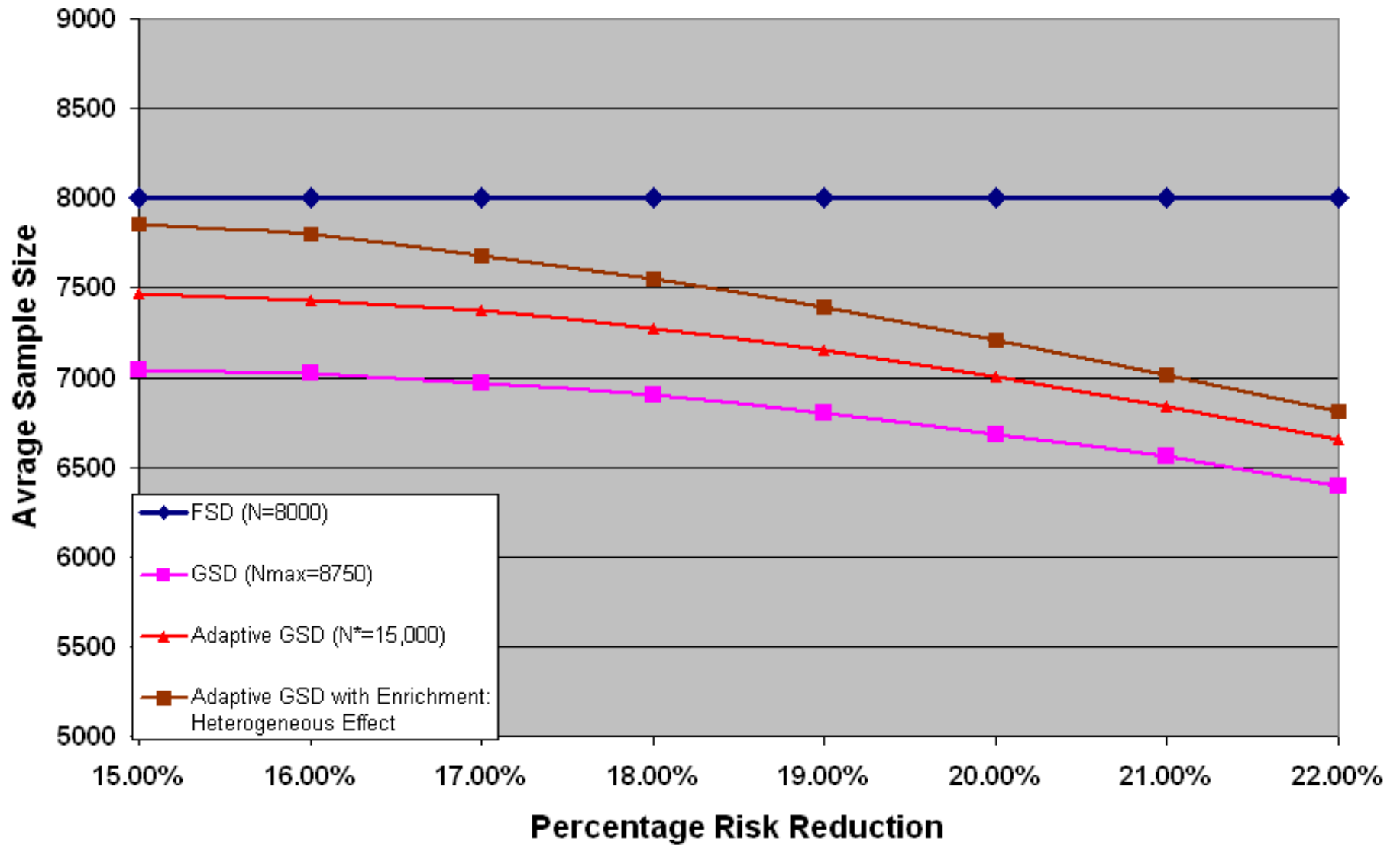
Power Curves for Fixed-Sample, Group Sequential, Group Sequential Adaptive and Enrichment Design Under Homogeneous and Heterogeneous Treatment Effect



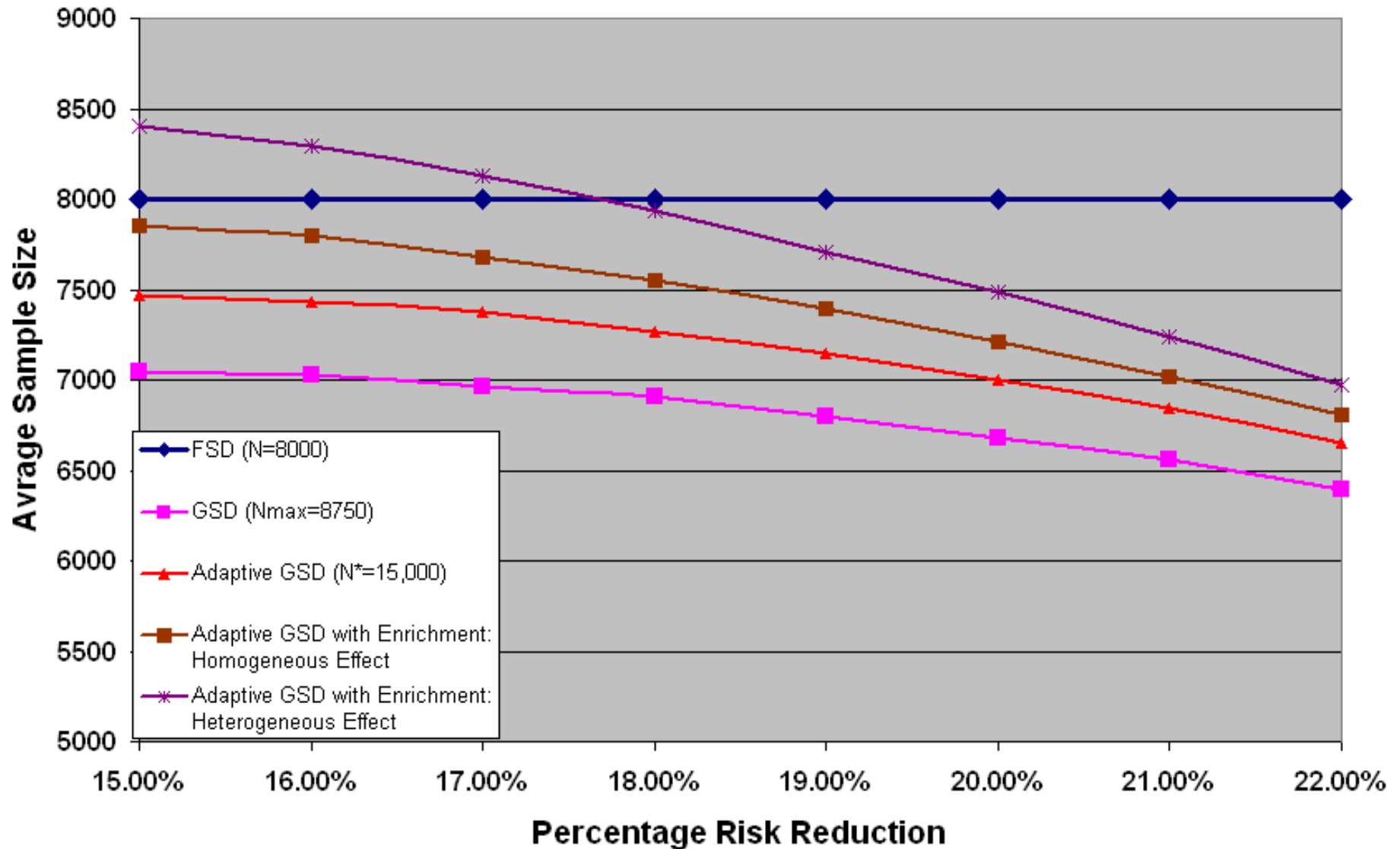
Average Sample Sizes for Fixed Sample, Group Sequential and Adaptive Group Sequential



Average Sample Sizes for Fixed Sample, Group Sequential Adaptive Group Sequential and Enrichment under Homogeneous Treatment Effect



Average Sample Sizes for Fixed Sample, Group Sequential, Adaptive Group Sequential, and Enrichment Designs under Homogeneous and Heterogeneous Treatment Effect



# Concluding Remarks

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- **Why not run two independent trials; exploratory and confirmatory?**
  - exploratory trial won't be adequately powered for subgroups
  - if it fails, there won't be any support for the confirmatory trial
  - current design contains an insurance policy for handling subgroups
- **Pre-specification of subgroups not a statistical requirement. But important safeguard against chasing random noise**
- **Flexibility to change sample size and enrich population greatly increases complexity of trial management**
  - Logistics of drug are complicated if sample size is increased at IA2
  - Recruitment might slow down if population is enriched at IA2
- **Sponsor cannot be involved in interim decision making. Must appoint independent committee with clinical and statistical expertise**
- **Simulate the design thoroughly before committing to it**